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Embedded Solar Tracker Design Utilizing Solar Position Calculation with Sensor Correction

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EMBEDDED SOLAR TRACKER DESIGN UTILIZING SOLAR POSITION CALCULATION
WITH SENSOR CORRECTION

by

AUSTIN MARTINEZ

GRADUATE PAPER

Submitted in partial fulfillment
of the requirements for the degree of
MASTER OF SCIENCE
in Electrical Engineering

Approved by:

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DEPARTMENT OF ELECTRICAL AND MICROELECTRONIC ENGINEERING
KATE GLEASON COLLEGE OF ENGINEERING
ROCHESTER INSTITUTE OF TECHNOLOGY
ROCHESTER, NEW YORK

MAY, 2023

Dedication

I dedicate this work to my mother Julie Martinez, my father Danny Martinez, my brother Aiden Martinez, and my great friends for their love and support during my time in college.

Austin Martinez

Declaration

I hereby declare that except where specific reference is made to the work of others, that all content of this Graduate Paper are original and have not been submitted in whole or in part for consideration for any other degree or qualification in this, or any other University. This Graduate Project is the result of my own work and includes nothing which is the outcome of work done in collaboration, except where specifically indicated in the text.

Austin Martinez

May, 2023

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Austin Martinez

Abstract

As renewable energy becomes more accessible, affordable optimization solutions have become a larger part of at home systems. Solar energy is one of the most common clean energy applications used by homeowners because of its increasing affordability. While many photovoltaic systems are statically mounted on roofs or in yards, many systems also employ some kind of solar tracking. Both single axis and dual axis solar tracking systems have been implemented and tested with multiple kinds of tracking methods. Two of the most accurate tracking strategies are utilizing light dependent resistors or using some kind of solar position calculation. This paper proposes a design for a solar tracking system that combines these two strategies, using a solar position algorithm to calculate the angle of the sun which is then corrected by light dependent resistors if necessary. This design is highly accurate as well as being robust in finding the sun regardless of weather conditions and geographical location. Data from two days of testing shows an average percent difference in solar energy output of 1.486% in the late evening and 0.883% near solar noon.

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Chapter 1

Introduction

Clean energy is an ever growing industry as it becomes both more energy efficient and more cost effective. Solar has quickly garnered a reputation as being one of the most popular choices of clean energy. Used by big businesses and homeowners alike, improvements can always be made to escalate the efficiency of solar panels for all applications. As more individuals acquire their own panels for private use, affordable optimization strategies are going to be needed.

Many homeowners already take advantage of static solar panels—solar panels that are placed at a permanent angle—however some may want to transition to a system that utilizes a solar tracking system. In theory, a solar panel utilizing a tracking system should absorb more solar energy than a static solar panel. This is discussed in more detail in Section 2. For that reason, people may want to make use of an affordable solar tracking system.

While the sun can be tracked numerous different ways, this project will test the reliability of using Global Positioning System (GPS) data to calculate the angle of the sun. This algorithm, discussed in more detail in Section 3, will use latitude, longitude, and time data from an embedded GPS module to calculate the angle of the sun from the current location. This is a more robust method than light detection, for example, as it is unaffected by cloud coverage.

1.1 Research Goals

The main goal of this design is to implement an affordable and efficient solar tracking system that absorbs more energy than static solar panels by combining two very robust solar tracking techniques. This design will be physically assembled using low-cost materials, as well as programmed in C on a STMicroelectronics (STM) development board. The solar tracking system will be compared to a non-tracking system to verify that the former does in fact increase the energy absorbed by the solar panel.

1.2 Organization

The structure of the paper is as follows:

- Section 2: This section discusses the concept of solar tracking and its comparison to static solar panels. It also speaks on previous work done in this area and how their results influenced this design.
- Section 3: This section covers the algorithm used for calculating the angle of the sun for this project.
- Section 4: This section explains the proposed physical architecture of the system as well as the structure of the software that will be used to control the entire system.
- Section 5: This section details the experiment setup and how the data is gathered for characterization.
- Section 6: This section discusses the data acquired from the experimental setup, namely the comparison between the energy absorption of the tracking system and the non-tracking system.

- Section 7: This section concludes the paper and outlines the possible directions for future work in this area.

Chapter 2

Bibliographical Research

This section discusses the value of solar tracking as a function of capturing solar energy as well as prior work in developing affordable Photovoltaics (PV) systems. Of the examples presented, some utilize some form of solar tracking, and some that do not.

2.1 The Concept of Solar Tracking

The goal of any clean energy system should be to generate as much energy as possible from the renewable source it is targeting. With solar energy, the most absorption occurs when the angle of incidence of the sun's rays is perpendicular to the solar panel [9]. Due to the way the sun passes through the sky as the day advances, the aforementioned angle of incidence is only perpendicular for a portion of the day. Because of this fact, PV systems that rely on a static solar panel are not absorbing all of the energy that could be captured throughout the course of the day. This situation has given way for the development of solar tracking systems that attempt to absorb as much energy as possible.

Solar tracking systems typically come in the following forms:

- Single axis tracker - Horizontal
- Single axis tracker - Vertical
- Dual axis tracker

Examples of these can be found in Figure 2.1.

Single axis trackers, coming in two main forms, try to angle the solar panel toward the sun while only being able to rotate on one axis. In the case of horizontal single axis trackers, the axis of rotation is parallel to the ground, typically rotating the solar panel from east to west as it follows the sun. In the case of vertical single axis trackers, the axis of rotation is perpendicular to the ground, spinning the solar panel like a top. This configuration usually involves a tilted solar panel as well. When compared to static solar panels, single axis tracking systems can perform upwards of 20% better in terms of daily output power [10]. While this higher performance and efficiency may have a higher upfront cost than a static solar panel, the higher energy output will add up over years and eventually save the user money [9]. For that reason, single axis trackers are a great option for a more optimized home PV system.

Dual axis trackers are an expansion on single axis trackers, wherein the two main configurations of single axis trackers are combined into one system. Therefore, the typical dual axis tracker has both a horizontal and vertical axis to rotate about, enabling more precise tracking. Where single axis trackers can be angled closer to the sun than a static solar tracker, they still do not maximize the absorption at all times of the day. Where single axis trackers are a good solution, dual axis trackers prove to be a more optimized solution. This claim is discussed further in Section 2.2 where prior work on solar trackers is covered, speaking on both single and dual axis tracking systems.

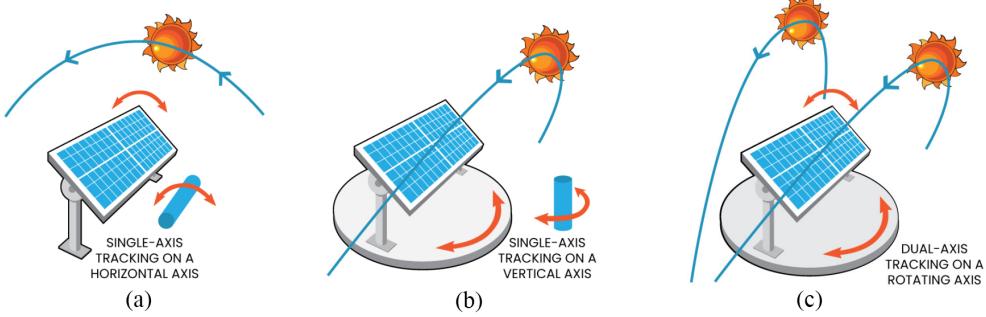


Figure 2.1: Three different types of solar trackers: (a) Single axis horizontal, (b) Single axis vertical, and (c) Dual axis [1, 2].

2.2 Prior Work

The problem of solar tracking has been approached before from many different angles. The prevailing strategies are typically one of the following or a combination of multiple:

- Light detection with light dependent resistor(s) (LDR)
- Angle calculation using Solar Position Algorithm (SPA)
- Maximum power point (MPP) detection
- Incrementally moving along a fixed path given known time and location data

All of these strategies have merit as solutions to solar tracking, however each comes with its own set of advantages and disadvantages.

Many designs implement one or more LDRs as part of the solar tracking system. For some, an LDR is used simply to detect whether the sun has risen or if it is night time. This implementation essentially wakes up the system so that the tracker can take over. For most others, however, the LDRs are used as a means for tracking the sun in the sky. This kind of tracking is usually done using two sensors in the case of single axis trackers, or four sensors in the case of dual axis trackers. The tracking is typically accomplished by placing the sensors in

an array and querying them on a regular basis. The resulting values are then used to determine which direction detected the greater light intensity. This determination is then used to move the solar panel in that direction until the values on the sensors are equal, indicating that the panel is pointing directly toward the sun. In single axis tracker experiments, the two LDRs are used to track the sun's movement from east to west throughout the day [9, 11]. With this tracking configuration, the north-south position can be adjusted manually as in [9], or not at all, depending on the desired results. If this angle is not changed by an outsider monthly, it may not be able to achieve maximum solar energy absorption as the sun's path through the sky changes. Nevertheless, these two single axis experiments saw a difference of about 1V of open circuit voltage, with the tracking system having the higher voltage output over the static setup. In a similar experiment that used a simulation that essentially mimicked the single axis two LDR system, similar improvements were seen [12]. In several cases of dual axis trackers using LDRs, the performance observed is even higher. For example, in one experiment that achieved solar tracking using only these sensors, both a single axis and dual axis setup were tested in parallel [10]. These authors found that the increased output power gain was increased by 23% using a single axis tracker, and 40% using a dual axis tracker. Even after accounting for the power used to move the motors, the increased power yield was high. Similar experiments [13, 14] employed the same kind of sensor array technique and observed equally promising results, demonstrating the reliability of LDR sensors in solar tracking. Additionally, the authors of [14] make a point that despite the system's best performance being on clearer days as opposed to cloudy, the performance over the course of a month still outdoes that of a static solar panel. Another related experiment employs the use of LDR sensing coupled with the MPP technique [15]. This setup utilized three sensors as well as four small solar panels as sensors in addition to the main solar panel. The four smaller solar panels are used as the four LDR sensors have been in the aforementioned experiments, using power generation

measurements rather than light intensity measurements. However, once the system reached the position calculated by the solar panels, the LDRs were used as a checking mechanism to ensure that the right position was found. If that was not the case, these sensors were used to correct the position. In this paper, this is the introduction of the use of LDRs as a means of correction. The MPP technique is also employed in [16] with the use of a single solar panel. The single axis system performs a periodic “current sweep” wherein the solar panel is swept across its range until the MPP is detected. The system then fixes the solar panel in this position until the next sweep. In other experiments [17, 18], authors paired the LDRs with a proportional-integral-derivative (PID) controller for more sophisticated sensor tracking. These two designs had great success in using these PID systems to track the sun accurately.

Another common technique employs the calculation of the solar position using the time and geographical location of the system. This strategy is used exclusively in [19, 20], and closely modeled in [21]. In [19, 20], single axis and dual axis respectively, a real-time clock (RTC) is used with the geographical location of the system hardcoded into the program to calculate the solar position. Both of these methods achieved success in solar tracking, however [19] made a point that the accuracy of the system is reliant on the accuracy of the mechanical setup. This implies that if at some point there occurs an error in the physical hardware, e.g. the motor housing, the accuracy of the RTC system declines. Because there are no other sensors on board to check the accuracy of the calculated position, the chance of faulty tracking becomes nonzero. Additionally, with both of these programs needing the geographical coordinates to be provided by an outsider or hardcoded, the system becomes less universally applicable. The same principle is used in [22, 23], where the geographical coordinates are provided to the system. However, these two implementations use LDRs as a corrective system for the solar position calculated by the SPA. This is similar to the principle introduced in [15] where the LDRs are used for corrective measures. Yet still, the systems require the coordinates to be

provided. While this is not inherently a bad result, it is more robust for the system to be able to determine the geographic location on its own. This leads to the GPS method presented in [24] that uses a GPS receiver to determine the time and geographic location. This information is then sent into the SPA which yields results that can point the solar panel toward the sun. The GPS system is then entirely self-sufficient, able to be moved to a different location and still calculate the correct solar position. This paper also presents a strictly timed method of solar tracking. In this mode, the system waits for the LDR to detect the beginning of the day, at which point the timer system begins moving the motor one degree every hour until the LDR detects that it is night time. This timed method is also implemented in [25] where the system moves every 30 minutes. While it does track the sun in these circumstances, this timer method is very application specific and not as universally applicable as the other methods.

Chapter 3

Solar Position Algorithm

A robust algorithm is required to reliably track the position of the sun in the sky. The National Renewable Energy Laboratory (NREL) has published the Solar Position Algorithm (SPA) that is used for many different applications today. This algorithm, valid for any time from the year -2000 to 6000 can be used to determine the solar zenith and azimuth angles with uncertainties of $\pm 0.0003^\circ$ [26]. With that, this is by far one of the most accurate algorithms for such a calculation, and an even more important tool for a solar tracking PV system. The following are the steps that are to be implemented in the proposed solar tracker design.

3.1 SPA Presented by NREL

The Solar Position Algorithm provided by NREL follows a very specific procedure to determine the relevant time and location data necessary to calculate the position of the sun. These steps are listed below and outlined in greater detail in [26].

- Calculate the Julian Day
- Calculate the Julian Ephemeris Day

- Calculate the Julian Century and the Julian Ephemeris Century
- Calculate the Julian Ephemeris Millennium
- Calculate the Earth heliocentric longitude, latitude, and radius vector
- Calculate the geocentric longitude and latitude
- Calculate the nutation in longitude and obliquity
- Calculate the true obliquity of the ecliptic
- Calculate the aberration correction
- Calculate the apparent sun longitude
- Calculate the apparent sidereal time at Greenwich at any given time
- Calculate the geocentric sun right ascension
- Calculate the geocentric sun declination
- Calculate the observer local hour angle
- Calculate the topocentric sun right ascension
- Calculate the topocentric local hour angle
- Calculate the topocentric zenith angle
- Calculate the topocentric azimuth angle
- Calculate the incidence angle for a surface oriented in any direction

3.2 SPA Programs

Algorithms for calculating the solar position have been implemented in programs before. A related solar position algorithm, The Grena's fifth algorithm, is implemented in Python 3.5 to achieve similar accuracy as the NREL algorithm in [8]. The drawback of this algorithm is that the validity only stretches from 2010 to 2110. Nonetheless, this implementation extracted input data from a GPS module. The only data needed from a GPS module to run the SPA is the UTC time and the geographical coordinates. This is demonstrated in the paper. The Python program uses the GPS data and runs their SPA calculation. The program achieved accurate results, calculating the solar angle within less than 0.5° and the solar azimuth angle within less than 0.1° [8]. This type of accuracy is more than acceptable for PV systems which brings confidence to the proposed design.

Another similar algorithm for determining the position of the sun is reviewed in [27]. This paper discusses several of the important parts of the calculation, what data is required, and what results from each of these parts. This is helpful in understanding the different parts of the SPA presented by NREL.

Chapter 4

System Architecture

The proposed design makes use of several of the strategies mentioned in Section 2.2 in an effort to make use of the techniques that have previously yielded positive results. This includes the utilization of the Solar Position Algorithm to calculate the azimuth and elevation angles for the motors to direct the solar panel towards. The information required for this calculation will be acquired through the use of a GPS device to ensure the system is more robust, as mentioned in Section 2.2. Additionally, LDRs are used to verify the solar position, correct the calculated position if necessary, as well as to detect if the sun has risen indicating that the system can wake up.

The design is comprised of both physical hardware and embedded software. The details of both of these parts are discussed in the next two subsections, first with a breakdown of the physical components that make up the hardware setup followed by a detailed explanation of the control program.

4.1 Hardware

The following are the different hardware components that have been used in the proposed design.

4.1.1 STM32 Nucleo-64 Development Board

This development board provides a well put together embedded platform to interface with all of the different components needed for this design. The board has an STM32L476RG microcontroller (MCU) with several useful peripherals such as timers, serial UART ports, ADCs, and DACs. This board will be powered using the USB port for the scope of this project, however in the future it is possible that this could run on energy generated by the solar panel.

4.1.2 MTK3339 GPS Module

The GPS module used for the proposed design is a small low-power chip that has a built-in antenna. The chip has been provided on a breakout board for ease of use and integration into the design. This breakout board also allows the ability to connect a coin cell battery to make use of the real-time clock (RTC) for warm starts. The chip prints out the GPS messages in serial UART using the NMEA 0183 sentence structure. This is discussed further in Section 4.2. For the purposes of this design, the only pins used are the VIN, GND, and TX. The TX pin, in this case, is the pin that transmits the output data from the GPS module to the Nucleo board.

4.1.3 MG996R Servo Motors

Two servo motors are necessary for the proposed design's dual axis tracking system. These motors are controlled by pulse width modulation (PWM). By sending a certain frequency to

the motor, it will turn to a certain angle. This control will allow for precise tracking of the sun. These two motors are held together in a 3D printed dual axis housing that allows for one of them to control the horizontal rotation and the other to control the vertical rotation. The solar panel is then mounted on the outer edge of the vertical motor.

4.1.4 Light Dependent Resistors (LDR)

The proposed design uses four LDRs for verifying and correcting the solar position calculated by the SPA. The LDRs used in the proposed design have a resistance range of $1\text{K}\Omega$ to $10\text{K}\Omega$. The resistance of these components change depending on the amount of light that the surface is exposed to. The four LDRs are placed in a diamond-like grid pointing in the same direction as the solar panel and are all separated by an opaque wall. This achieves independent readings by each sensor such that if they are facing at an angle away from the sun, some of them are in the light and some of them are in the dark. This produces a measurable difference in their respective resistance values which then allows for the determination of the true direction of the sun. If the sensors all have marginally similar readings, however, this verifies that the solar panel is pointed in the direction of the sun.

4.1.5 Solar Panel

The solar panel used for the proposed design is a smaller solar panel, capable of 100 mA at 5 V . This small solar panel is chosen to have a smaller load on the servo motors as well as the ADC on the Nucleo board.

4.2 Software

The flow of the control program is shown in Figure 4.1. The relevant source files can be seen in Appendix B. The control program consists of three main operations: wake up detection, solar tracking, and sunset detection.

4.2.1 Wake Up Detection

This part of the program is responsible for determining when the sun comes up and the day has started. This is done by regularly querying the LDRs to see if the measured light value suggests that the sun has risen. If the sun is not yet detected, the system goes back into deep sleep for another 30 minutes, when the sensors will be queried once again.

4.2.2 Solar Tracking

This component makes up the majority of the control program. Once the system has woken up, the GPS module will be queried for the first time using the `GPS_receive` function. The function works by reading the serial UART output from the GPS module until a full NMEA sentence is detected. The function then checks if the sentence received was of the GA type or RMC type. If it is not, the function will continue to read the serial UART output and check until the GA sentence is detected. If the GA sentence is detected, the `parseGGA` function is called which will decode the sentence and extract all of the data that it sent, as shown in Table 4.1. The same occurs for the case of detecting the RMC sentence, the breakdown of which can be seen in Table 4.2. Once the GPS data has been parsed, the function is exited and the data is passed to the SPA calculation. This function takes in the UTC time, latitude, and longitude, and returns a zero if the calculation was done without errors. From this, the zenith angle and azimuth angle are used to calculate the PWM values necessary to angle the

two servo motors correctly. These values are then sent to the corresponding timer channels which effectively moves the motors to the desired locations. From there, the LDRs are queried to determine if the calculated angle is correct. This is done by checking that all four LDRs have values that are marginally similar to each other. If the differences between the values are within a predetermined threshold, the function returns. If the difference between two values is greater than a predetermined threshold, then their values are used to correct the position. This correction is done as shown in Figure [LDR code snippet]. The motors are moved in the direction of greater light values until the LDR readings are within the difference threshold once again. Once the solar panel positioning is finished being determined, the system enters a wait period. During this wait period, the system collects solar energy for five minutes. At the end of this period, the system runs the sunset detection, as shown in Figure 4.1.

4.2.3 Sunset Detection

This part of the program is done at the end of every loop of the main solar tracking functionality. After each wait period, the LDR sensors are queried to get light values. These values are then checked to see whether they are less than a valid value, indicating that the sun is no longer high enough in the sky to be used. If this is true, the system resets the motor positions, enters a deep sleep, and goes back into the wake up detection functionality. Otherwise, the system goes back to the top of the solar tracking as shown in Figure 4.1.

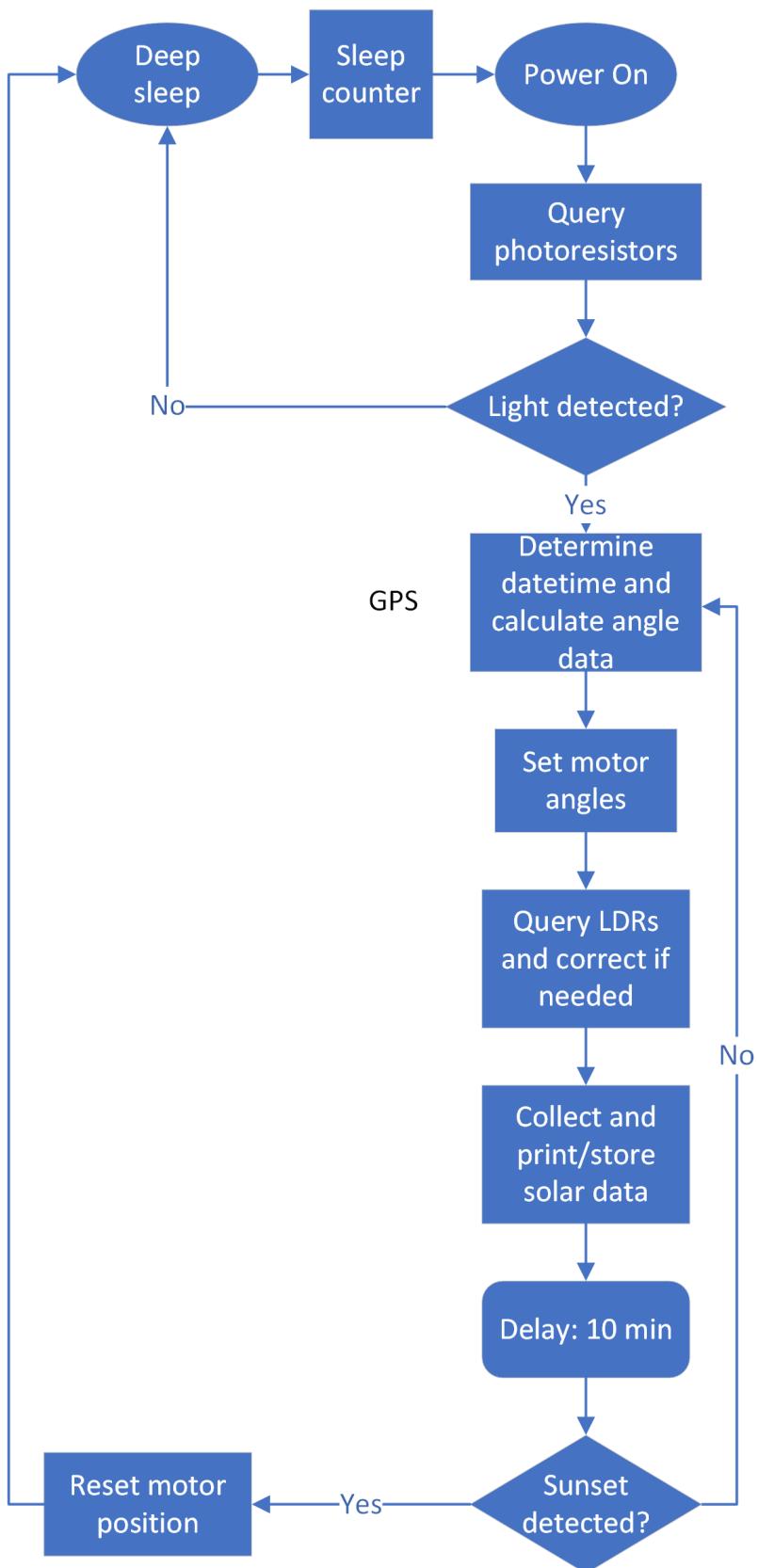


Figure 4.1: Program overview flowchart

Table 4.1: GPS GGA NMEA sentence structure [8]

Data	Structure
UTC time of position fix	hhmmss.ss
Latitude	ddmm.mmmm
Hemispherical Orientation N/S	n
Longitude	dddmm.mmmm
Hemispherical Orientation W/E	w
Type of position fix	x
Number of satellites used	y
Horizontal dilution of precision	z.z
Sea level altitude	aaaa.a
Altitude units	m
Geoidal separation	g.g
Geoidal separation units	m

Table 4.2: GPS RMC NMEA sentence structure [8]

Data	Structure
UTC time of position fix	hhmmss.ss
Status	a
Latitude	ddmm.mmmm
Hemispherical Orientation N/S	n
Longitude	dddmm.mmmm
Hemispherical Orientation W/E	w
Speed over ground (knots)	z.z
Track made good (degrees)	y.y
UTC date of position fix	ddmmyy
Magnetic Variation (degrees)	d.d
Variation Sense	v

Chapter 5

Experimental Setup

This section discusses the physical experimental setup, the type of data collected, and how the data is collected.

5.1 Physical Setup

The proposed design is assembled as shown in Figure 5.1. The ST Nucleo-64 development board receives 5 V power from a laptop. The board distributes 5 V power to the two MG996R servo motors and 3.3 V power to the GPS device and the LDRs. The UART TX port of the GPS device is connected to the UART1 RX port of the development board to receive the NMEA sentences containing the GPS data. The four LDRs are being pulled up to 3.3 V using $1K\Omega$ resistors. The LDR values are being probed on the net between the LDR and the pull-up resistor for each, labeled as LDR n where $n \in \{1, 2, 3, 4\}$. These probes are wired into four channels of ADC1 on the development board. The ADC converts the voltage into a digital value that is used in the program. The servo motors' PWM lines are connected to Timer 3 Channel 1 and Channel 2 ports on the development board. This is how the motors receive

PWM signals that control their positions. The two servo motors are placed in a dual axis housing that allows them to rotate to any solar angle necessary. The fixture that holds the solar panel and the LDR circuit is attached to the vertical motor as that is the one that will point the fixture toward the sun. Additionally, a voltage divider is used to scale the output voltage of the solar panel from 5.5 V to 3.5 V as the reference voltage for the development board is 3.5 V. This scaled output voltage is connected to another input channel of ADC1 on the development board. The schematic for this physical setup is shown in Figure 5.2

5.2 Data Collection

The relevant data collected from the experimental setup includes the output voltage of the solar panel and the accuracy of the GPS calculated positioning. Two key data points are collected for the output voltage at each newly calculated position. The first data point is the output voltage of the solar panel in the position calculated by the proposed design. The second data point is the output voltage of the solar panel pointed straight up into the sky, simulating a static solar panel. The accuracy of the GPS calculated positioning is also tracked each time the system moves the panel to a newly determined position. This is a binary data point detecting whether the calculated position is pointing the solar panel directly at the sun or not. Finally, the date and time is collected at each new position to understand how the data changes throughout the day.

5.3 Procedure

The system is tested using the physical setup described above. The solar tracking system is placed in one spot for a duration of time, allowing the system to run and continuously collect

data. All of the data is printed to a terminal using UART and continually logged in a text file.

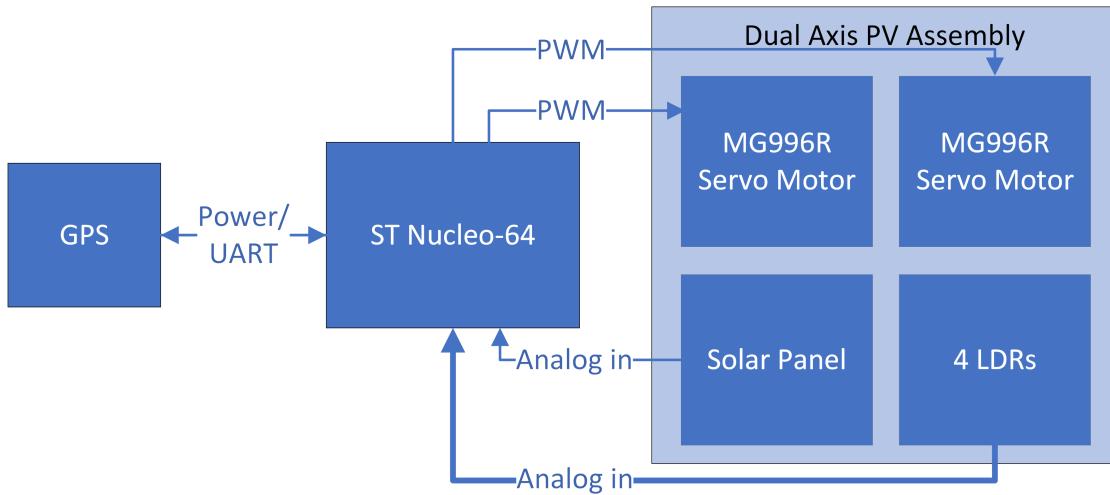


Figure 5.1: Experimental setup of proposed design.

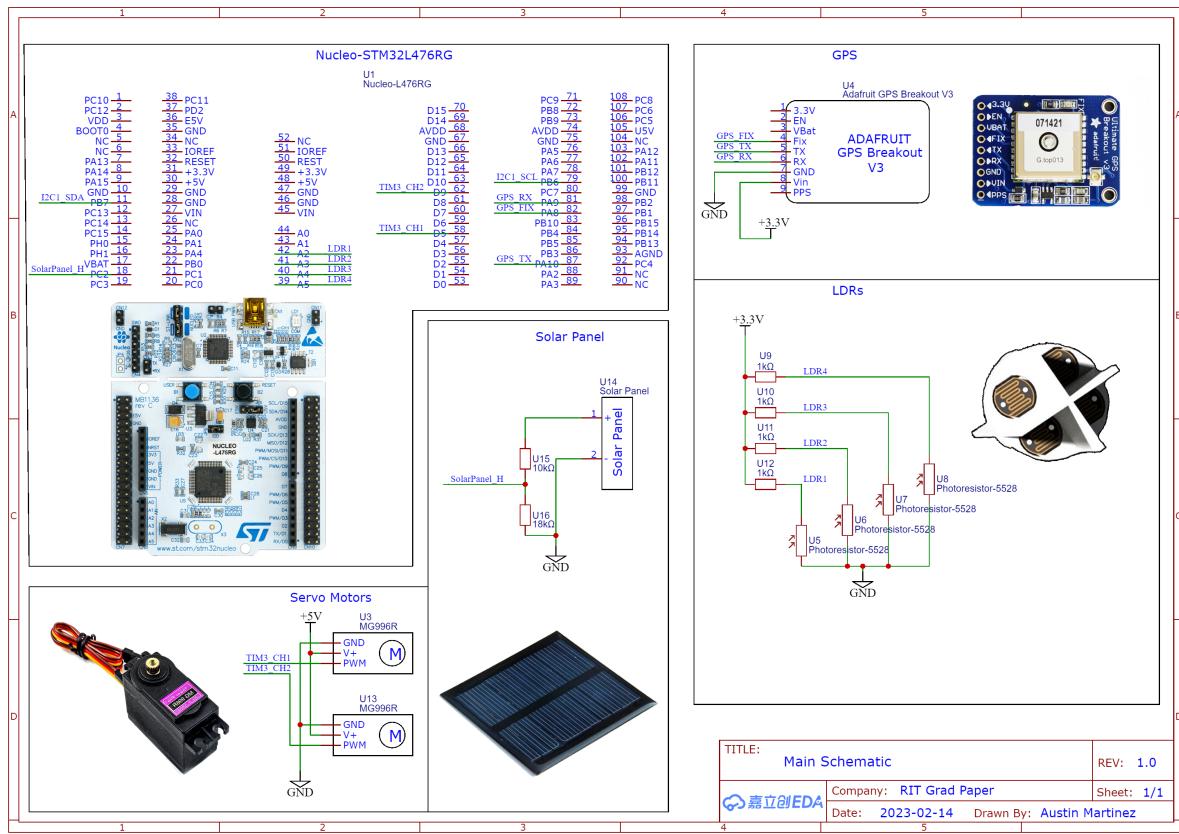


Figure 5.2: Schematic of the physical setup, describing the connections between each device [3-7].

Chapter 6

Results and Discussion

The results of the experiment and analyses of the results is provided in this chapter.

6.1 Solar Data

The experimental setup was run for a total of 116 minutes over two days where the weather was partly sunny. The solar data collected from these two days is shown in Figures 6.1 and 6.2. The solar data collected on May 1 covers the times between 5:23 PM and 6:56 PM Eastern Time (ET). As shown in the graph, the sun is declining at this time of the day. This is evident from the decreasing values collected for the Output Voltage as the time progresses. The solar data collected on May 2 covers the times between 1:01 PM and 1:16 PM ET. As shown in this graph, the sun is almost directly above the experimental setup as the solar data does not change very much in the time interval. This is confirmed as the SPA calculated the solar noon—the time when the sun reaches its highest point in the sky—to be at 1:08 PM on May 2. In both figures, the solar energy being absorbed in the position calculated by the SPA is represented by the blue line, whereas the solar energy being absorbed by the simulated static solar panel is

represented by the red line. Both figures show that the output voltage of both positions is quite similar for most of the duration of the test. Table 6.1 shows that the average percent difference of the output voltage of the two solar panel positions is less than two percent for both days' data.

SPA vs. Static Output Voltage May 1, 2023

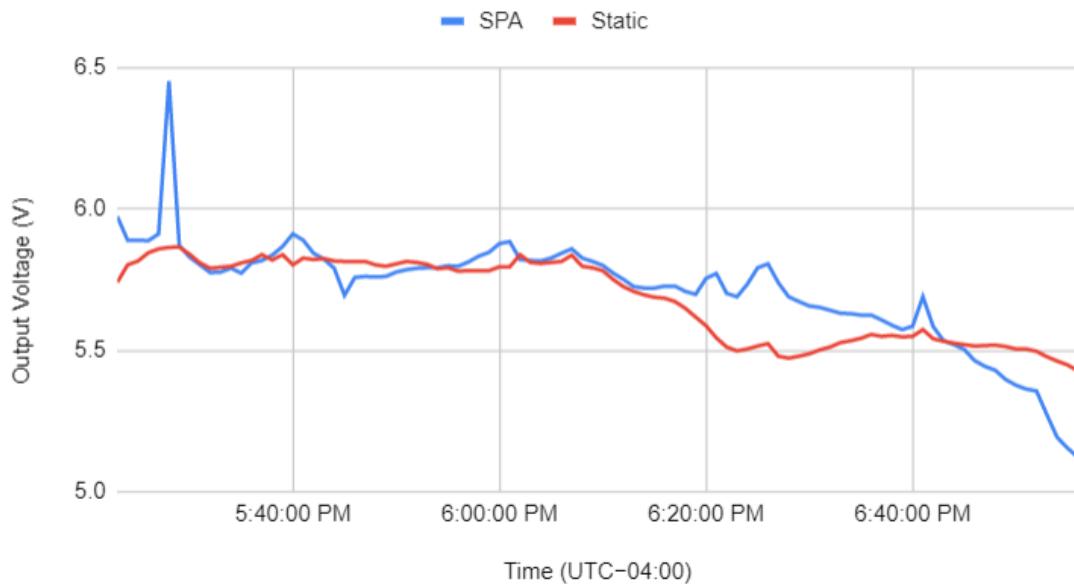


Figure 6.1: Solar data collected on May 1, 2023.

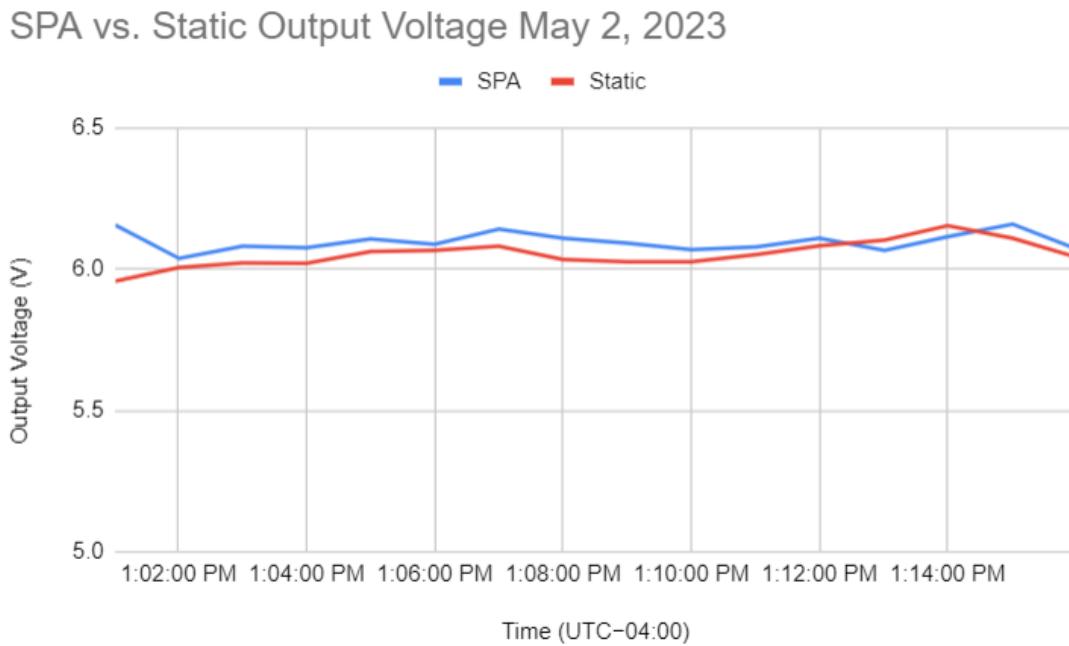


Figure 6.2: Solar data collected on May 2, 2023.

Table 6.1: Average Percent Difference SPA vs. Static Output Voltage

Day	Average Percent Difference
May 1, 2023	1.486%
May 2, 2023	0.883%

Chapter 7

Conclusion

This paper proposes a design for a Photovoltaics system that uses GPS data coupled with a Solar Position Algorithm to increase the energy output. The system accomplishes this by accurately tracking the position of the sun and aiming the solar panel in that direction, maximizing the possible solar absorption. This position is then checked using light dependent resistors to ensure that the calculated position is true. Solar tracker systems have been proposed in many different forms, as was described earlier in this paper, however this design combines the accuracy of precise calculations with the reliability of self-checking. The data shows that the solar tracking is accurate and that the energy output is improved.

The goal of the research was to create an affordable and easy-to-use system that would accurately track the sun. The proposed design is programmed in C on an affordable development board. The entire system, with the exception of the solar panel, can be assembled for just over \$100. Other than assembly, the most a user would need to change would be the UTC offset.

7.1 Future Work

While the work described in this paper was largely successful, there are multiple areas where the proposed design can be improved. A few suggestions for possible improvements are as follows:

- The program is written specifically for the STM32 Nucleo-L476RG, which has a pin layout and peripheral setup that may differ from other STM development boards. The program can be expanded to support other development boards.
- While the system was proven to outperform a static solar panel, the size of the panel used in the experimental setup may have limited the results. A future experimental setup could utilize a larger solar panel that may yield better results.
- The current program is only configurable by editing the code. The design could be expanded to be configured in some sort of user interface, either through a serial terminal, screen, or otherwise.
- The GPS device used in the proposed design is accurate and provides data within 30 seconds or after 5 minutes, depending on the weather conditions. A future iteration of the design could use an external antenna to get GPS data faster if weather conditions prove to be a problem.
- The experimental setup was not tested in harsh conditions like rain or snow. This could be useful data to acquire.

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Appendix I

Source Code

I.1 Main Header File

```
1 /* USER CODE BEGIN Header */
2 /**
3  ****
4 * @file          : main.h
5 * @brief         : Header for main.c file.
6 *                   This file contains the common defines of
7 *                   the application.
8 *
9 *
10 * Copyright (c) 2023 STMicroelectronics.
```



```
30 #include "stm3214xx_hal.h"  
31  
32 /* Private includes  
-----  
 */  
33 /* USER CODE BEGIN Includes */  
34  
35 /* USER CODE END Includes */  
36  
37 /* Exported types  
-----  
 */  
38 /* USER CODE BEGIN ET */  
39  
40 /* USER CODE END ET */  
41  
42 /* Exported constants  
----- */  
43 /* USER CODE BEGIN EC */  
44  
45 /* USER CODE END EC */  
46  
47 /* Exported macro  
-----  
 */
```

```
48 /* USER CODE BEGIN EM */  
49  
50 /* USER CODE END EM */  
51  
52 void HAL_TIM_MspPostInit(TIM_HandleTypeDef *htim);  
53  
54 /* Exported functions prototypes  
-----*/  
55 void Error_Handler(void);  
56  
57 /* USER CODE BEGIN EFP */  
58  
59 /* USER CODE END EFP */  
60  
61 /* Private defines  
-----*/  
62 #define B1_Pin GPIO_PIN_13  
63 #define B1_GPIO_Port GPIOC  
64 #define PR4_Pin GPIO_PIN_0  
65 #define PR4_GPIO_Port GPIOC  
66 #define PR3_Pin GPIO_PIN_1  
67 #define PR3_GPIO_Port GPIOC  
68 #define USART_TX_Pin GPIO_PIN_2  
69 #define USART_TX_GPIO_Port GPIOA
```

```
70 #define USART_RX_Pin GPIO_PIN_3
71 #define USART_RX_GPIO_Port GPIOA
72 #define PR1_Pin GPIO_PIN_4
73 #define PR1_GPIO_Port GPIOA
74 #define LD2_Pin GPIO_PIN_5
75 #define LD2_GPIO_Port GPIOA
76 #define PR2_Pin GPIO_PIN_0
77 #define PR2_GPIO_Port GPIOB
78 #define GPS_FIX_Pin GPIO_PIN_8
79 #define GPS_FIX_GPIO_Port GPIOA
80 #define GPS_TX_Pin GPIO_PIN_10
81 #define GPS_TX_GPIO_Port GPIOA
82 #define TMS_Pin GPIO_PIN_13
83 #define TMS_GPIO_Port GPIOA
84 #define TCK_Pin GPIO_PIN_14
85 #define TCK_GPIO_Port GPIOA
86 #define SWO_Pin GPIO_PIN_3
87 #define SWO_GPIO_Port GPIOB
88 /* USER CODE BEGIN Private defines */
89
90 /* USER CODE END Private defines */
91
92 #ifdef __cplusplus
93 }
94#endif
```

95

96 #endif /* __MAIN_H */

Listing I.1: Main Header File

I.2 Main Solar Tracker Program

```
1 /* USER CODE BEGIN Header */

2 /**
3 ****
4 * @file          : main.c
5 * @brief         : Main program body
6 ****

7 * @attention
8 *
9 * Copyright (c) 2023 STMicroelectronics .
10 * All rights reserved .
11 *
12 * This software is licensed under terms that can be found in
13 * the LICENSE file
14 * in the root directory of this software component .
15 * If no LICENSE file comes with this software , it is
16 * provided AS-IS .
17 */
18 /* USER CODE END Header */
```

```
19 /* Includes
-----
 * /
20 #include "main.h"
21
22 /* Private includes
-----
 * /
23 /* USER CODE BEGIN Includes */
24 #include <stdio.h>
25 #include <string.h>
26 #include <stdlib.h>
27 #include "MTK3339.h"
28 #include "PCA9685.h"
29 #include "SPA.h"
30 /* USER CODE END Includes */
31
32 /* Private typedef
-----
 * /
33 /* USER CODE BEGIN PTD */
34
35 /* USER CODE END PTD */
36
```

```
37 /* Private define
-----
 * /
38 /* USER CODE BEGIN PD */
39 // #define DEBUG_PRINT 1
40 /* USER CODE END PD */
41
42 /* Private macro
-----
 * /
43 /* USER CODE BEGIN PM */
44
45 /* USER CODE END PM */
46
47 /* Private variables
-----
 */
```

48 ADC_HandleTypeDef hadc1 ;
49 ADC_HandleTypeDef hadc2 ;
50 DMA_HandleTypeDef hdma_adc1 ;
51 DMA_HandleTypeDef hdma_adc2 ;
52
53 I2C_HandleTypeDef hi2c1 ;
54
55 TIM_HandleTypeDef htim2 ;
56 TIM_HandleTypeDef htim3 ;

```
57
58 UART_HandleTypeDef huart1;
59 UART_HandleTypeDef huart2;
60
61 /* USER CODE BEGIN PV */
62
63 uint32_t ADC_raw_values[4] = {0,0,0,0}; // raw ADC converted
   values
64 float PR_values[4] = {0,0,0,0};      // ADC values converted
   to voltages
65 uint32_t solar_panel_raw = 0;        // raw solar panel ADC value
66 float solar_panel_voltage = 0;       // Solar panel voltage
67
68 int programState = 0; // program state in state machine
69 int last_time = 0;    // temp variable to hold last GPS time
70 int isSunUp = 0;     // 0 if sun is down, 1 if sun is up
71
72 // enumerated states for FSM
73 enum States
74 {
75 Startup, // initialization, first GPS acquire
76 Running, // general operation throughout the day
77 Sleep    // no operation, checking for sunrise
78 };
79
```

```
80 // motor variables
-----
81 typedef struct
82 {
83     int UL;      // upper limit value for motor
84     int LL;      // lower limit value for motor
85     int pos;     // current position of motor
86     int altitude; // calculated altitude of motor, translated
                     // from SPA
87     int azimuth; // calculated azimuth of motor, translated
                     // from SPA
88 } motor;
89
90 motor motor1 = { // horizontal, uses azimuth
91     .UL = 190,
92     .LL = 10,
93 };
94
95 motor motor2 = { // vertical, uses altitude
96     .UL = 190,
97     .LL = 10,
98 };
99
100 // gps variables
-----
```

```
101 extern struct GgaType gga; // instance of GPS gga data
    structure
102 extern struct RmcType rmc; // instance of GPS rmc data
    strcuture
103
104 // spa variables
-----
105 spa_data spa = { // instance of SPA data structure
106     .delta_ut1 = 0,
107     .delta_t = 37,
108     .timezone = -4,
109     .pressure = 2068.43, // average annual pressure in
                           Rochester, NY is 30in
110     .temperature = 9.167, // average annual temperature is 48.5
                           F
111     .atmos_refract = 0.5667,
112     .azm_rotation = 0, // if i am in global village aiming at
                           Salsarita's
113     .slope = 0,
114     .function = 1
115 };
116
117
118 /* USER CODE END PV */
119
```

```
120 /* Private function prototypes
-----*/
121 void SystemClock_Config(void);
122 void PeriphCommonClock_Config(void);
123 static void MX_GPIO_Init(void);
124 static void MX_DMA_Init(void);
125 static void MX_USART2_UART_Init(void);
126 static void MX_I2C1_Init(void);
127 static void MX_TIM2_Init(void);
128 static void MX_USART1_UART_Init(void);
129 static void MX_ADC1_Init(void);
130 static void MX_TIM3_Init(void);
131 static void MX_ADC2_Init(void);
132 /* USER CODE BEGIN PFP */
133 extern void GPS_Init();
134 extern void GPS_receive();
135 /* USER CODE END PFP */
136
137 /* Private user code
-----*/
138 /* USER CODE BEGIN 0 */
139
140 // function prototype for moving the motors , defined at bottom
141 // of file
142 int moveServo(int motor, int position);
```

```
142
143 /**
144 * Use the ADC to read the solar panel voltage.
145 * Convert it into scaled voltage value.
146 */
147 void getSolarPanelVoltage( void )
148 {
149     HAL_ADC_Start_DMA(&hadc2 , &solar_panel_raw , 1);      // start
150     HAL_Delay(2000);
151     solar_panel_voltage = solar_panel_raw * (3.5 / 4096) * 2; // convert to voltage value
152 }
153
154 /**
155 * Use the ADC to read the LDR values.
156 * Convert them into voltage values.
157 * Value decreases as light increases.
158 */
159 void readLightSensors( void )
160 {
161     HAL_ADC_Start_DMA(&hadc1 , ADC_raw_values , 4);      // start
162     ADC1 in DMA mode, point it to PR array
163     for( int val=0; val<4; val++)
164     {
```

```
164     PR_values[ val ] = ADC_raw_values[ val ] * ( 3.5 / 4096 ); //  
165     convert to voltage value  
166 }  
167  
168 /**  
169 * Check if the motor position is valid.  
170 * Return 0 if no correction is needed.  
171 * Otherwise, correct the position using LDRs  
172 * and return 1.  
173 */  
174 int correctPosition( void )  
175 {  
176     // first check if they are all equal, in which case no  
     correction is needed  
177     if( ( abs( PR_values[0] - PR_values[1] ) < 0.5 ) &&  
178         ( abs( PR_values[0] - PR_values[2] ) < 0.5 ) &&  
179         ( abs( PR_values[0] - PR_values[3] ) < 0.5 ) )  
180     {  
181         return 0;  
182     }  
183     else  
184     {  
185         // correct the position  
186         int balanced = 0; // are LDR values roughly equal?
```

```
187
188     while (! balanced)
189     {
190         readLightSensors ();
191
192         if ( ( abs ( PR_values [0] - PR_values [1]) < 0.5) &&
193             ( abs ( PR_values [0] - PR_values [2]) < 0.5) &&
194             ( abs ( PR_values [0] - PR_values [3]) < 0.5) )
195         {
196             balanced = 1;
197         }
198     else
199     {
200         // average value of LDRs in each direction
201         int top    = (ADC_raw_values [0] + ADC_raw_values [1]) /
202                         2;
203         int bottom = (ADC_raw_values [2] + ADC_raw_values [3]) /
204                         2;
205         int left   = (ADC_raw_values [0] + ADC_raw_values [2]) /
206                         2;
207         int right  = (ADC_raw_values [1] + ADC_raw_values [3]) /
208                         2;
209
210         if ((top - bottom) > 0)
211         {
```

```
208         moveServo(1, motor1.pos + 2);  
209     }  
210     else if((top - bottom) < 0)  
211     {  
212         moveServo(1, motor1.pos - 2);  
213     }  
214     else if((left - right) > 0)  
215     {  
216         moveServo(2, motor1.pos - 2);  
217     }  
218     else if((left - right) < 0)  
219     {  
220         moveServo(1, motor1.pos + 2);  
221     }  
222     }  
223 }  
224 return 1;  
225 }  
226 }  
227  
228 /**  
229 * Calculate motor angles from SPA results  
230 * spa: spa handle with the results  
231 */  
232 void calculateMotorsPos(spa_data *sspa)
```

```
233  {
234      // calculate servo value for solar azimuth
235      int az = spa.azimuth; // azimuth adjusted to motor range
236      int ze = spa.zenith; // zenith adjusted to motor range
237
238      if (az >= 0 && az < 90) // northeast
239      {
240          az = az + 90;
241          motor1.azimuth = (int)(115 - ((az*97)/180));
242          motor2.altitude = (int)(65 - ((ze*47.5)/90)); // bend
243              backwards
244      }
245      else if (az >= 90 && az < 270) // south
246      {
247          az = az - 90;
248          motor1.azimuth = (int)(115 - ((az*97)/180));
249          motor2.altitude = (int)(65 + ((ze*47.5)/90)); // bend
250              forwards
251      }
252      else if (az >= 270) // south
253      {
254          az = az - 270;
255          motor1.azimuth = (int)(115 - ((az*97)/180));
256          motor2.altitude = (int)(65 - ((ze*47.5)/90)); // bend
257              backwards
```

```
255      }
256  }
257
258 /* USER CODE END 0 */
259
260 /**
261 * @brief  The application entry point.
262 * @retval int
263 */
264 int main( void )
265 {
266 /* USER CODE BEGIN 1 */
267
268 /* USER CODE END 1 */
269
270 /* MCU Configuration
-----
 * /
271
272 /* Reset of all peripherals , Initializes the Flash interface
   and the Systick . */
273 HAL_Init();
274
275 /* USER CODE BEGIN Init */
276
```

```
277  /* USER CODE END Init */  
278  
279  /* Configure the system clock */  
280  SystemClock_Config();  
281  
282  /* Configure the peripherals common clocks */  
283  PeriphCommonClock_Config();  
284  
285  /* USER CODE BEGIN SysInit */  
286  
287  /* USER CODE END SysInit */  
288  
289  /* Initialize all configured peripherals */  
290  MX_GPIO_Init();  
291  MX_DMA_Init();  
292  MX_USART2_UART_Init();  
293  MX_I2C1_Init();  
294  MX_TIM2_Init();  
295  MX_USART1_UART_Init();  
296  MX_ADC1_Init();  
297  MX_TIM3_Init();  
298  MX_ADC2_Init();  
299  /* USER CODE BEGIN 2 */  
300  GPS_Init();  
301  /* USER CODE END 2 */
```

```
302
303     /* Infinite loop */
304     /* USER CODE BEGIN WHILE */
305     char str[100] = "System Start\r\n";
306     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str),
307                         HAL_MAX_DELAY);
308     memset(&str, 0, sizeof(str));
309
310     // Start Timer 3 and
311     HAL_TIM_Base_Start(&htim3);
312     HAL_TIM_PWM_Start(&htim3, TIM_CHANNEL_1); // start servo 1
313         CH1 PB4 D5 (18 to 115)
314     HAL_TIM_PWM_Start(&htim3, TIM_CHANNEL_2); // start servo 2
315         CH2 PC7 D9 (18 to 113 is 180 degrees)
316
317
318     while (1)
319     {
320         // beginning of startup state
321         -----
322         while (programState == Startup)
```

```

323
324 #ifdef DEBUG_PRINT
325     sprintf(str, "GPS Query\r\n");
326     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str),
327                         HAL_MAX_DELAY);
328     memset(&str, 0, sizeof(str));
329
330     while (gga.fix == 0) // query the GPS until we get
331         valid GGA data
332
333
334 #ifdef DEBUG_PRINT
335     sprintf(str, "Time: %d : %d : %d\r\n"
336             "Latitude:      %0.4f%c\r\n"
337             "Longitude:     %0.4f%c\r\n"
338             "Fix:           %d\r\n"
339             "Satellites:    %d\r\n",
340             gga.hours, gga.minutes, gga.seconds,
341             gga.latitude_adj, gga.nsIndicator,
342             gga.longitude_adj, gga.ewIndicator,
343             gga.fix, gga.satellites);
344
345     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str),
346                         HAL_MAX_DELAY); // print the GPS data

```

```
345     memset(&str , 0 , sizeof(str));  
346 #endif  
347  
348 }  
349 while (rmc.status != 'A') // query the GPS until we get  
    valid RMC data  
350 {  
351     GPS_receive(); // get the data from the GPS module  
352 }  
353  
354 last_time = gga.minutes;  
355 // insert data to PCA calculator  
356 spa.longitude = getLongitudeAsDegrees();  
357 spa.latitude = getLatitudeAsDegrees();  
358 spa.elevation = gga.altitude;  
359 spa.year = rmc.year;  
360 spa.month = rmc.month;  
361 spa.day = rmc.day;  
362 spa.hour = (gga.hours - 4); // subtract 4 for the UTC  
    offset for current location  
363 spa.minute = gga.minutes;  
364 spa.second = gga.seconds;  
365  
366 programState = Running;
```

```
367     } // end of startup state
-----
368
369     // beginning of general operation state
-----
370     while(programState == Running)
371     {
372         // get new GPS data
373         while(gga.minutes == last_time)
374         {
375             GPS_receive();
376         }
377
378         last_time = gga.minutes;
379         // insert data to PCA calculator
380         spa.longitude = getLongitudeAsDegrees();
381         spa.latitude = getLatitudeAsDegrees();
382         spa.elevation = gga.altitude;
383         spa.year = rmc.year;
384         spa.month = rmc.month;
385         spa.day = rmc.day;
386         spa.hour = (gga.hours - 4); // subtract 4 for the UTC
387             offset for current location
388         spa.minute = gga.minutes;
389         spa.second = gga.seconds;
```

```
389
390     // run the SPA calculation
391     if (spa_calculate(&spa) == 0)
392     {
393
394 #ifdef DEBUG_PRINT
395     sprintf(str, "SPA calculated\r\n");
396     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str),
397                       HAL_MAX_DELAY);
398     memset(&str, 0, sizeof(str));
399
400     // point the motors
401     calculateMotorsPos(&spa); // calculate motor positions
402     from SPA results
403
404 #ifdef DEBUG_PRINT
405     sprintf(str, "motor 1 angle: %d\r\n"
406             "motor 2 angle: %d\r\n",
407             motor1.azimuth, motor2.altitude);
408     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str),
409                       HAL_MAX_DELAY);
410     memset(&str, 0, sizeof(str));
411
412 #endif
413
414 }
```

```
411     moveServo(1, motor1.azimuth);
412     moveServo(2, motor2.altitude);
413
414 #ifdef DEBUG_PRINT
415     sprintf(str, "Motors moved\r\n");
416     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str),
417                         HAL_MAX_DELAY);
418     memset(&str, 0, sizeof(str));
419
420     HAL_Delay(5000); // wait for 5 second for solar panel
421                         to get some sun
422
423     getSolarPanelVoltage();
424     // print solar panel voltage
425     sprintf(str, "Time: %d : %d : %d\r\n"
426             "SPA Output Voltage = %0.4f\r\n", (gga.hours - 4),
427             gga.minutes, gga.seconds, solar_panel_voltage);
428
429     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str)
430                         , HAL_MAX_DELAY);
431     memset(&str, 0, sizeof(str));
432
433     // then check the position with the LDRs
434     readLightSensors();
435
436     if(correctPosition() == 0)
```

```
432     {  
433         sprintf(str , "Accurate\r\n");  
434         HAL_UART_Transmit(&huart2 , (uint8_t *)str , sizeof(  
435             str) , HAL_MAX_DELAY);  
436         memset(&str , 0, sizeof(str));  
437     }  
438     else  
439     {  
440         sprintf(str , "NOT Accurate\r\n");  
441         HAL_UART_Transmit(&huart2 , (uint8_t *)str , sizeof(  
442             str) , HAL_MAX_DELAY);  
443         memset(&str , 0, sizeof(str));  
444     }  
445     // check to see if the sun is still in the sky  
446     for( int ii=0; i<4; i++)  
447     {  
448         if( ADC_raw_values[ ii ] > 3000)  
449         {  
450             isSunUp = 0;  
451             programState = Sleep;  
452         }  
453     }  
454     // make solar panel flat
```

```
455     moveServo(2, 65);  
456  
457     HAL_Delay(5000); // wait for 1 second for solar panel  
        to get some sun  
458  
459     getSolarPanelVoltage();  
460     // print solar panel voltage  
461     sprintf(str, "Static Output Voltage = %0.4f\r\n",  
        solar_panel_voltage);  
462     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(str)  
        , HAL_MAX_DELAY);  
463     memset(&str, 0, sizeof(str));  
464 } // end of SPA operation  
465  
466     HAL_Delay(10000); // wait 10 sec before reading again  
467 } // end of running state  
  
-----  
468  
469 // beginning of sleep state  
  
-----  
470 while(programState == Sleep)  
471 {  
472     // sleep for 30 minutes  
473     HAL_Delay(180000);  
474     // check LDRs for sunrise
```

```
475     readLightSensors();  
476     for(int i i=0; i<4; i++)  
477     {  
478         if(ADC_raw_values[ i i ] <= 3000)  
479         {  
480             isSunUp = 1;  
481             programState = Startup;  
482         }  
483     }  
484  
485 } // end of sleep state  
  
-----  
486  
487 /* USER CODE END WHILE */  
488  
489 /* USER CODE BEGIN 3 */  
490 }  
491 /* USER CODE END 3 */  
492 }  
493  
494 /**  
495 * @brief System Clock Configuration  
496 * @retval None  
497 */  
498 void SystemClock_Config(void)
```

```
499  {
500      RCC_OscInitTypeDef RCC_OscInitStruct = {0};
501      RCC_ClkInitTypeDef RCC_ClkInitStruct = {0};
502
503      /** Configure the main internal regulator output voltage
504      */
505      if (HAL_PWREx_ControlVoltageScaling(
506          PWR_REGULATOR_VOLTAGE_SCALE1) != HAL_OK)
507      {
508          Error_Handler();
509      }
510
511      /** Initializes the RCC Oscillators according to the
512      * specified parameters
513      * in the RCC_OscInitTypeDef structure.
514
515      RCC_OscInitStruct.OscillatorType = RCC_OSCILLATORTYPE_HSI;
516      RCC_OscInitStruct.HSISState = RCC_HSI_ON;
517      RCC_OscInitStruct.HSICalibrationValue =
518          RCC_HSICALIBRATION_DEFAULT;
519
520      RCC_OscInitStruct.PLL.PLLState = RCC_PLL_ON;
521      RCC_OscInitStruct.PLL.PLLSource = RCC_PLLSOURCE_HSI;
522      RCC_OscInitStruct.PLL.PLLM = 1;
523      RCC_OscInitStruct.PLL.PLLN = 10;
524      RCC_OscInitStruct.PLL.PLLP = RCC_PLLP_DIV7;
```

```
521     RCC_OscInitStruct.PLL.PLLQ = RCC_PLLQ_DIV2;
522     RCC_OscInitStruct.PLL.PLLR = RCC_PLLR_DIV2;
523     if (HAL_RCC_OscConfig(&RCC_OscInitStruct) != HAL_OK)
524     {
525         Error_Handler();
526     }
527
528     /** Initializes the CPU, AHB and APB buses clocks
529 */
530     RCC_ClkInitStruct.ClockType = RCC_CLOCKTYPE_HCLK|
531                                     |RCC_CLOCKTYPE_PCLK1|
532                                     |RCC_CLOCKTYPE_PCLK2;
533
534     RCC_ClkInitStruct.SYSCLKSource = RCC_SYSCLKSOURCE_PLLCLK;
535     RCC_ClkInitStruct.AHBCLKDivider = RCC_SYSCLK_DIV1;
536     RCC_ClkInitStruct.APB1CLKDivider = RCC_HCLK_DIV8;
537     RCC_ClkInitStruct.APB2CLKDivider = RCC_HCLK_DIV1;
538
539     if (HAL_RCC_ClockConfig(&RCC_ClkInitStruct, FLASH_LATENCY_4)
540         != HAL_OK)
541     {
542         Error_Handler();
543     }
544 }
```

```
543  /**
544   * @brief Peripherals Common Clock Configuration
545   * @retval None
546   */
547 void PeriphCommonClock_Config(void)
548 {
549     RCC_PeriphCLKInitTypeDef PeriphClkInit = {0};
550
551     /** Initializes the peripherals clock
552     */
553     PeriphClkInit.PeriphClockSelection = RCC_PERIPHCLK_ADC;
554     PeriphClkInit.AdcClockSelection = RCC_ADCCLKSOURCE_PLLSAI1;
555     PeriphClkInit.PLLSAI1.PLLSAI1Source = RCC_PLLSOURCE_HSI;
556     PeriphClkInit.PLLSAI1.PLLSAI1M = 1;
557     PeriphClkInit.PLLSAI1.PLLSAI1N = 8;
558     PeriphClkInit.PLLSAI1.PLLSAI1P = RCC_PLLP_DIV7;
559     PeriphClkInit.PLLSAI1.PLLSAI1Q = RCC_PLLQ_DIV2;
560     PeriphClkInit.PLLSAI1.PLLSAI1R = RCC_PLLR_DIV2;
561     PeriphClkInit.PLLSAI1.PLLSAI1ClockOut = RCC_PLLSAI1_ADC1CLK;
562     if (HAL_RCCEx_PeriphCLKConfig(&PeriphClkInit) != HAL_OK)
563     {
564         Error_Handler();
565     }
566 }
567
```

```
568  /**
569   * @brief ADC1 Initialization Function
570   * @param None
571   * @retval None
572   */
573 static void MX_ADC1_Init(void)
574 {
575
576 /* USER CODE BEGIN ADC1_Init_0 */
577
578 /* USER CODE END ADC1_Init_0 */
579
580 ADC_MultiModeTypeDef multimode = {0};
581 ADC_ChannelConfTypeDef sConfig = {0};
582
583 /* USER CODE BEGIN ADC1_Init_1 */
584
585 /* USER CODE END ADC1_Init_1 */
586
587 /**
588  * Common config
589  */
590 hadc1.Instance = ADC1;
591 hadc1.Init.ClockPrescaler = ADC_CLOCK_ASYNC_DIV1;
592 hadc1.Init.Resolution = ADC_RESOLUTION_12B;
593 hadc1.Init.DataAlign = ADC_DATAALIGN_RIGHT;
```

```
593     hadc1.Init.ScanConvMode = ADC_SCAN_ENABLE;
594     hadc1.Init.EOCSelection = ADC_EOC_SINGLE_CONV;
595     hadc1.Init.LowPowerAutoWait = DISABLE;
596     hadc1.Init.ContinuousConvMode = DISABLE;
597     hadc1.Init.NbrOfConversion = 4;
598     hadc1.Init.DiscontinuousConvMode = DISABLE;
599     hadc1.Init.ExternalTrigConv = ADC_SOFTWARE_START;
600     hadc1.Init.ExternalTrigConvEdge =
601         ADC_EXTERNALTRIGCONVEDGE_NONE;
602     hadc1.Init.DMAContinuousRequests = DISABLE;
603     hadc1.Init.Overrun = ADC_OVR_DATA_PRESERVED;
604     hadc1.Init.OversamplingMode = DISABLE;
605     if (HAL_ADC_Init(&hadc1) != HAL_OK)
606     {
607         Error_Handler();
608     }
609     /**
610      * Configure the ADC multi-mode
611      */
612     multimode.Mode = ADC_MODE_INDEPENDENT;
613     if (HAL_ADCEx_MultiModeConfigChannel(&hadc1, &multimode) != HAL_OK)
614     {
615         Error_Handler();
616     }
```

```
616
617     /** Configure Regular Channel
618     */
619     sConfig.Channel = ADC_CHANNEL_9;
620     sConfig.Rank = ADC_REGULAR_RANK_1;
621     sConfig.SamplingTime = ADC_SAMPLETIME_6CYCLES_5;
622     sConfig.SingleDiff = ADC_SINGLE_ENDED;
623     sConfig.OffsetNumber = ADC_OFFSET_NONE;
624     sConfig.Offset = 0;
625     if (HAL_ADC_ConfigChannel(&hadc1, &sConfig) != HAL_OK)
626     {
627         Error_Handler();
628     }
629
630     /** Configure Regular Channel
631     */
632     sConfig.Channel = ADC_CHANNEL_15;
633     sConfig.Rank = ADC_REGULAR_RANK_2;
634     if (HAL_ADC_ConfigChannel(&hadc1, &sConfig) != HAL_OK)
635     {
636         Error_Handler();
637     }
638
639     /** Configure Regular Channel
640     */
```

```
641     sConfig.Channel = ADC_CHANNEL_2;
642     sConfig.Rank = ADC_REGULAR_RANK_3;
643     if (HAL_ADC_ConfigChannel(&hadc1, &sConfig) != HAL_OK)
644     {
645         Error_Handler();
646     }
647
648     /* * Configure Regular Channel
649     */
650     sConfig.Channel = ADC_CHANNEL_1;
651     sConfig.Rank = ADC_REGULAR_RANK_4;
652     if (HAL_ADC_ConfigChannel(&hadc1, &sConfig) != HAL_OK)
653     {
654         Error_Handler();
655     }
656     /* USER CODE BEGIN ADC1_Init_2 */
657
658     /* USER CODE END ADC1_Init_2 */
659
660 }
661
662 /**
663 * @brief ADC2 Initialization Function
664 * @param None
665 * @retval None
```

```
666     */
667 static void MX_ADC2_Init(void)
668 {
669
670     /* USER CODE BEGIN ADC2_Init_0 */
671
672     /* USER CODE END ADC2_Init_0 */
673
674     ADC_ChannelConfTypeDef sConfig = {0};
675
676     /* USER CODE BEGIN ADC2_Init_1 */
677
678     /* USER CODE END ADC2_Init_1 */
679
680     /**
681      * Common config
682
683     hadc2.Instance = ADC2;
684     hadc2.Init.ClockPrescaler = ADC_CLOCK_ASYNC_DIV1;
685     hadc2.Init.Resolution = ADC_RESOLUTION_12B;
686     hadc2.Init.DataAlign = ADC_DATAALIGN_RIGHT;
687     hadc2.Init.ScanConvMode = ADC_SCAN_DISABLE;
688     hadc2.Init.EOCSelection = ADC_EOC_SINGLE_CONV;
689     hadc2.Init.LowPowerAutoWait = DISABLE;
690     hadc2.Init.ContinuousConvMode = DISABLE;
691     hadc2.Init.NbrOfConversion = 1;
```

```
691     hadc2 . Init . DiscontinuousConvMode = DISABLE;
692     hadc2 . Init . ExternalTrigConv = ADC_SOFTWARE_START;
693     hadc2 . Init . ExternalTrigConvEdge =
694         ADC_EXTERNALTRIGCONVEDGE_NONE;
695     hadc2 . Init . DMAContinuousRequests = DISABLE;
696     hadc2 . Init . Overrun = ADC_OVR_DATA_PRESERVED;
697     hadc2 . Init . OversamplingMode = DISABLE;
698     if (HAL_ADC_Init(&hadc2) != HAL_OK)
699     {
700         Error_Handler();
701     }
702     /* Configure Regular Channel
703     */
704     sConfig.Channel = ADC_CHANNEL_16;
705     sConfig.Rank = ADC_REGULAR_RANK_1;
706     sConfig.SamplingTime = ADC_SAMPLETIME_6CYCLES_5;
707     sConfig.SingleDiff = ADC_SINGLE_ENDED;
708     sConfig.OffsetNumber = ADC_OFFSET_NONE;
709     sConfig.Offset = 0;
710     if (HAL_ADC_ConfigChannel(&hadc2, &sConfig) != HAL_OK)
711     {
712         Error_Handler();
713     }
714     /* USER CODE BEGIN ADC2_Init_2 */
```

```
715
716     /* USER CODE END ADC2_Init_2 */
717
718 }
719
720 /**
721 * @brief I2C1 Initialization Function
722 * @param None
723 * @retval None
724 */
725 static void MX_I2C1_Init(void)
726 {
727
728     /* USER CODE BEGIN I2C1_Init_0 */
729
730     /* USER CODE END I2C1_Init_0 */
731
732     /* USER CODE BEGIN I2C1_Init_1 */
733
734     /* USER CODE END I2C1_Init_1 */
735     hi2c1.Instance = I2C1;
736     hi2c1.Init.Timing = 0x00202538;
737     hi2c1.Init.OwnAddress1 = 0;
738     hi2c1.Init.AddressingMode = I2C_ADDRESSINGMODE_7BIT;
739     hi2c1.Init.DualAddressMode = I2C_DUALADDRESS_DISABLE;
```

```
740     hi2c1.Init.OwnAddress2 = 0;  
741     hi2c1.Init.OwnAddress2Masks = I2C_OA2_NOMASK;  
742     hi2c1.Init.GeneralCallMode = I2C_GENERALCALL_DISABLE;  
743     hi2c1.Init.NoStretchMode = I2C_NOSTRETCH_DISABLE;  
744     if (HAL_I2C_Init(&hi2c1) != HAL_OK)  
745     {  
746         Error_Handler();  
747     }  
748  
749     /** Configure Analogue filter  
750     */  
751     if (HAL_I2CEx_ConfigAnalogFilter(&hi2c1,  
752                                         I2C_ANALOGFILTER_ENABLE) != HAL_OK)  
753     {  
754         Error_Handler();  
755     }  
756     /** Configure Digital filter  
757     */  
758     if (HAL_I2CEx_ConfigDigitalFilter(&hi2c1, 0) != HAL_OK)  
759     {  
760         Error_Handler();  
761     }  
762     /* USER CODE BEGIN I2C1_Init_2 */  
763 
```

```
764     /* USER CODE END I2C1_Init_2 */  
765  
766 }  
767  
768 /**  
769  * @brief TIM2 Initialization Function  
770  * @param None  
771  * @retval None  
772  */  
773 static void MX_TIM2_Init(void)  
774 {  
775  
776     /* USER CODE BEGIN TIM2_Init_0 */  
777  
778     /* USER CODE END TIM2_Init_0 */  
779  
780     TIM_MasterConfigTypeDef sMasterConfig = {0};  
781     TIM_OC_InitTypeDef sConfigOC = {0};  
782  
783     /* USER CODE BEGIN TIM2_Init_1 */  
784  
785     /* USER CODE END TIM2_Init_1 */  
786     htim2.Instance = TIM2;  
787     htim2.Init.Prescaler = 0;  
788     htim2.Init.CounterMode = TIM_COUNTERMODE_UP;
```

```
789     htim2.Init.Period = 4294967295;
790     htim2.Init.ClockDivision = TIM_CLOCKDIVISION_DIV1;
791     htim2.Init.AutoReloadPreload =
792         TIM_AUTORELOAD_PRELOAD_DISABLE;
793     if (HAL_TIM_PWM_Init(&htim2) != HAL_OK)
794     {
795         Error_Handler();
796     sMasterConfig.MasterOutputTrigger = TIM_TRGO_RESET;
797     sMasterConfig.MasterSlaveMode = TIM_MASTERSLAVEMODE_DISABLE;
798     if (HAL_TIMEx_MasterConfigSynchronization(&htim2, &
799         sMasterConfig) != HAL_OK)
800     {
801         Error_Handler();
802     sConfigOC.OCMode = TIM_OCMODE_PWM1;
803     sConfigOC.Pulse = 0;
804     sConfigOC.OCPolarity = TIM_OCPOLARITY_HIGH;
805     sConfigOC.OCFastMode = TIM_OCFAST_DISABLE;
806     if (HAL_TIM_PWM_ConfigChannel(&htim2, &sConfigOC,
807         TIM_CHANNEL_1) != HAL_OK)
808     {
809         Error_Handler();
810     /* USER CODE BEGIN TIM2_Init_2 */

```

```
811
812     /* USER CODE END TIM2_Init_2 */
813     HAL_TIM_MspPostInit(&htim2);
814
815 }
816
817 /**
818 * @brief TIM3 Initialization Function
819 * @param None
820 * @retval None
821 */
822 static void MX_TIM3_Init(void)
823 {
824
825     /* USER CODE BEGIN TIM3_Init_0 */
826
827     /* USER CODE END TIM3_Init_0 */
828
829     TIM_ClockConfigTypeDef sClockSourceConfig = {0};
830     TIM_MasterConfigTypeDef sMasterConfig = {0};
831     TIM_OC_InitTypeDef sConfigOC = {0};
832
833     /* USER CODE BEGIN TIM3_Init_1 */
834
835     /* USER CODE END TIM3_Init_1 */
```

```
836     htim3.Instance = TIM3;
837     htim3.Init.Prescaler = 400;
838     htim3.Init.CounterMode = TIM_COUNTERMODE_UP;
839     htim3.Init.Period = 1000;
840     htim3.Init.ClockDivision = TIM_CLOCKDIVISION_DIV1;
841     htim3.Init.AutoReloadPreload =
842         TIM_AUTORELOAD_PRELOAD_DISABLE;
843     if (HAL_TIM_Base_Init(&htim3) != HAL_OK)
844     {
845         Error_Handler();
846         sClockSourceConfig.ClockSource = TIM_CLOCKSOURCE_INTERNAL;
847         if (HAL_TIM_ConfigClockSource(&htim3, &sClockSourceConfig)
848             != HAL_OK)
849         {
850             Error_Handler();
851             if (HAL_TIM_PWM_Init(&htim3) != HAL_OK)
852             {
853                 Error_Handler();
854             }
855             sMasterConfig.MasterOutputTrigger = TIM_TRGO_RESET;
856             sMasterConfig.MasterSlaveMode = TIM_MASTERSLAVEMODE_DISABLE;
857             if (HAL_TIMEx_MasterConfigSynchronization(&htim3, &
858                 sMasterConfig) != HAL_OK)
```

```
858     {
859         Error_Handler();
860     }
861     sConfigOC.OCMode = TIM_OCMODE_PWM1;
862     sConfigOC.Pulse = 0;
863     sConfigOC.OCPolarity = TIM_OCPOLARITY_HIGH;
864     sConfigOC.OCFastMode = TIM_OCFAST_DISABLE;
865     if (HAL_TIM_PWM_ConfigChannel(&htim3, &sConfigOC,
866                                     TIM_CHANNEL_1) != HAL_OK)
867     {
868         Error_Handler();
869     }
870     if (HAL_TIM_PWM_ConfigChannel(&htim3, &sConfigOC,
871                                     TIM_CHANNEL_2) != HAL_OK)
872     {
873         Error_Handler();
874     }
875     /* USER CODE BEGIN TIM3_Init_2 */
876     HAL_TIM_MspPostInit(&htim3);
877
878 }
879
880 /**
```

```
881     * @brief USART1 Initialization Function
882     * @param None
883     * @retval None
884     */
885 static void MX_USART1_UART_Init(void)
886 {
887
888     /* USER CODE BEGIN USART1_Init_0 */
889
890     /* USER CODE END USART1_Init_0 */
891
892     /* USER CODE BEGIN USART1_Init_1 */
893
894     /* USER CODE END USART1_Init_1 */
895     huart1.Instance = USART1;
896     huart1.Init.BaudRate = 9600;
897     huart1.Init.WordLength = UART_WORDLENGTH_8B;
898     huart1.Init.StopBits = UART_STOPBITS_1;
899     huart1.Init.Parity = UART_PARITY_NONE;
900     huart1.Init.Mode = UART_MODE_TX_RX;
901     huart1.Init.HwFlowCtl = UART_HWCONTROL_NONE;
902     huart1.Init.OverSampling = UART_OVERSAMPLING_16;
903     huart1.Init.OneBitSampling = UART_ONE_BIT_SAMPLE_DISABLE;
904     huart1.AdvancedInit.AdvFeatureInit =

```

UART_ADVFEATURE_RXOVERRUNDISABLE_INIT;

```
905     huart1.AdvancedInit.OverrunDisable =
906         UART_ADVFEATURE_OVERRUN_DISABLE;
907     if (HAL_UART_Init(&huart1) != HAL_OK)
908     {
909         Error_Handler();
910     /* USER CODE BEGIN USART1_Init_2 */
911
912     /* USER CODE END USART1_Init_2 */
913
914 }
915
916 /**
917 * @brief USART2 Initialization Function
918 * @param None
919 * @retval None
920 */
921 static void MX_USART2_UART_Init(void)
922 {
923
924     /* USER CODE BEGIN USART2_Init_0 */
925
926     /* USER CODE END USART2_Init_0 */
927
928     /* USER CODE BEGIN USART2_Init_1 */
```

```
929
930     /* USER CODE END USART2_Init 1 */
931
932     huart2.Instance = USART2;
933
934     huart2.Init.BaudRate = 115200;
935
936     huart2.Init.WordLength = UART_WORDLENGTH_8B;
937
938     huart2.Init.StopBits = UART_STOPBITS_1;
939
940     huart2.Init.Parity = UART_PARITY_NONE;
941
942     huart2.Init.Mode = UART_MODE_TX_RX;
943
944     huart2.Init.HwFlowCtl = UART_HWCONTROL_NONE;
945
946     huart2.Init.OverSampling = UART_OVERSAMPLING_16;
947
948     huart2.Init.OneBitSampling = UART_ONE_BIT_SAMPLE_DISABLE;
949
950     huart2.AdvancedInit.AdvFeatureInit = UART_ADVFEATURE_NO_INIT
951
952     ;
953
954     if (HAL_UART_Init(&huart2) != HAL_OK)
955     {
956         Error_Handler();
957     }
958
959     /* USER CODE BEGIN USART2_Init 2 */
960
961     /* USER CODE END USART2_Init 2 */
962
963
964     }
965
966
967     /**
968      * Enable DMA controller clock
969
970      */
```

```
953     */
954 static void MX_DMA_Init( void )
955 {
956
957     /* DMA controller clock enable */
958     __HAL_RCC_DMA1_CLK_ENABLE();
959
960     /* DMA interrupt init */
961     /* DMA1_Channel1_IRQHandler interrupt configuration */
962     HAL_NVIC_SetPriority(DMA1_Channel1_IRQn, 0, 0);
963     HAL_NVIC_EnableIRQ(DMA1_Channel1_IRQn);
964     /* DMA1_Channel2_IRQHandler interrupt configuration */
965     HAL_NVIC_SetPriority(DMA1_Channel2_IRQn, 0, 0);
966     HAL_NVIC_EnableIRQ(DMA1_Channel2_IRQn);
967
968 }
969
970 /**
971 * @brief GPIO Initialization Function
972 * @param None
973 * @retval None
974 */
975 static void MX_GPIO_Init( void )
976 {
977     GPIO_InitTypeDef GPIO_InitStruct = {0};
```

```
978
979     /* GPIO Ports Clock Enable */
980     __HAL_RCC_GPIOC_CLK_ENABLE();
981     __HAL_RCC_GPIOH_CLK_ENABLE();
982     __HAL_RCC_GPIOA_CLK_ENABLE();
983     __HAL_RCC_GPIOB_CLK_ENABLE();
984
985     /* Configure GPIO pin Output Level */
986     HAL_GPIO_WritePin(LD2_GPIO_Port, LD2_Pin, GPIO_PIN_RESET);
987
988     /* Configure GPIO pin : B1_Pin */
989     GPIO_InitStruct.Pin = B1_Pin;
990     GPIO_InitStruct.Mode = GPIO_MODE_IT_FALLING;
991     GPIO_InitStruct.Pull = GPIO_NOPULL;
992     HAL_GPIO_Init(B1_GPIO_Port, &GPIO_InitStruct);
993
994     /* Configure GPIO pin : LD2_Pin */
995     GPIO_InitStruct.Pin = LD2_Pin;
996     GPIO_InitStruct.Mode = GPIO_MODE_OUTPUT_PP;
997     GPIO_InitStruct.Pull = GPIO_NOPULL;
998     GPIO_InitStruct.Speed = GPIO_SPEED_FREQ_LOW;
999     HAL_GPIO_Init(LD2_GPIO_Port, &GPIO_InitStruct);
1000
1001    /* Configure GPIO pin : GPS_FIX_Pin */
1002    GPIO_InitStruct.Pin = GPS_FIX_Pin;
```

```
1003     GPIO_InitStruct.Mode = GPIO_MODE_INPUT;
1004     GPIO_InitStruct.Pull = GPIO_NOPULL;
1005     HAL_GPIO_Init(GPS_FIX_GPIO_Port, &GPIO_InitStruct);
1006
1007 }
1008
1009 /* USER CODE BEGIN 4 */
1010
1011 /**
1012 * Move servo motor to a position.
1013 * motor:      the motor to be moved.
1014 * position:   the position to move the motor to.
1015 * Return 0 if inputs are valid.
1016 * Return 1 if inputs are invalid.
1017 */
1018 int moveServo(int motor, int position)
1019 {
1020     if(motor == 1)
1021     {
1022         if(position < motor1.UL && position > motor1.LL) // if
1023             {
1024                 TIM3->CCR1 = position; // change PWM to position
1025                 motor1.pos = position; // update current motor position
1026                 return 0; // no errors
```

```
1027      }
1028      else
1029      {
1030          return 1; // invalid position input
1031      }
1032  }
1033  else if(motor == 2)
1034  {
1035      if(position < motor2.UL && position > motor2.LL) // if
1036      {
1037          TIM3->CCR2 = position; // change PWM to position
1038          motor2.pos = position; // update current motor position
1039          return 0; // no errors
1040      }
1041  else
1042  {
1043      return 1; // invalid position input
1044  }
1045  }
1046  else
1047  {
1048      return 1; // invalid motor input
1049  }
1050 }
```

```
1051
1052
1053
1054
1055
1056
1057 /* USER CODE END 4 */
1058
1059 /**
1060 * @brief This function is executed in case of error
1061 * occurrence.
1062 */
1063 void Error_Handler(void)
1064 {
1065 /* USER CODE BEGIN Error_Handler_Debug */
1066 /* User can add his own implementation to report the HAL
1067 error return state */
1068 __disable_irq();
1069 {
1070 }
1071 /* USER CODE END Error_Handler_Debug */
1072 }
1073
```

```
1074 #ifdef USE_FULL_ASSERT
1075 /**
1076 * @brief Reports the name of the source file and the source
1077 * line number
1078 * @param file: pointer to the source file name
1079 * @param line: assert_param error line source number
1080 * @retval None
1081 */
1082 void assert_failed(uint8_t *file, uint32_t line)
1083 {
1084 /* USER CODE BEGIN 6 */
1085 /* User can add his own implementation to report the file
1086 name and line number,
1087 ex: printf("Wrong parameters value: file %s on line %d\r\
1088 n", file, line) */
1089 /* USER CODE END 6 */
1090 }
```

Listing I.2: Main Source File

I.3 MTK3339 GPS Header File

```
1 #ifndef MTK3339_H
2 #define MTK3339_H
3
4 /**
5  * An interface to the MTK3339 GPS module.
6  */
7
8 /*
9  * MTK3339.h
10 *
11 * The original C++ code has been provided by
12 * EmbeddedArtists on mbed.com
13 * https://os.mbed.com/users/embeddedartists/code/MTK3339/
14 *
15 * The following source file has been ported
16 * to C as well as modified to interact with the STM32
17 * platform.
18 *
19 * Ported and expanded on: Mar 21, 2023
20 * Author: Austin Martinez
21 */
22
23 enum NmeaSentence
```

```
24     {
25         NmeaInvalid = 0,
26         NmeaGga = 0x01,
27 //         NmeaGsa = 0x02,
28 //         NmeaGsv = 0x04,
29 //         NmeaRmc = 0x08,
30         NmeaVtg = 0x10
31     };
32
33     struct GgaType {
34         /** UTC time - hours */
35         int hours;
36         /** UTC time - minutes */
37         int minutes;
38         /** UTC time - seconds */
39         int seconds;
40         /** UTC time - milliseconds */
41         int milliseconds;
42
43         /** The latitude in ddmm.mmmm format (d = degrees, m =
44             minutes) */
44         double latitude;
45         /** The longitude in dddmm.mmmm format */
46         double longitude;
47         /** North / South indicator */
47 }
```

```
48     char nsIndicator;
49     /** East / West indicator */
50     char ewIndicator;
51     /** Latitude adjusted to be in dd.dddd format */
52     double latitude_adj;
53     /** Longitude adjusted to be in dd.dddd format */
54     double longitude_adj;
55
56     /**
57      * Position indicator:
58      * 0 = Fix not available
59      * 1 = GPS fix
60      * 2 = Differential GPS fix
61      */
62     int fix;
63
64     /** Number of used satellites */
65     int satellites;
66     /** Horizontal Dilution of Precision */
67     double hdop;
68     /** antenna altitude above/below mean sea-level */
69     double altitude;
70     /** geoidal separation */
71     double geoidal;
72 }
```

```
73
74
75     struct RmcType {
76         /** UTC time - hours */
77         int hours;
78         /** UTC time - minutes */
79         int minutes;
80         /** UTC time - seconds */
81         int seconds;
82         /** UTC time - milliseconds */
83         int milliseconds;
84
85         /** Status Indicator:
86          * A = data valid
87          * V = data NOT valid
88          */
89         char status;
90
91         /** The latitude in ddmm.mmmm format (d = degrees, m =
92             minutes) */
93         double latitude;
94         /** The longitude in dddmm.mmmm format */
95         double longitude;
96         /** North / South indicator */
97         char nsIndicator;
```

```
97         /** East / West indicator */
98         char ewIndicator;
99
100        /** Speed over ground - knots */
101        double speed;
102
103        /** Course over ground - knots */
104        double course;
105
106        /** UTC Date - year */
107        int year;
108
109        /** UTC Date - month */
110        int month;
111
112        /** UTC Date - day */
113        int day;
114
115    };
116
117
118    struct VtgType {
119
120        /** heading in degrees */
121        double course;
122
123        /** speed in Knots */
124        double speedKnots;
125
126        /** Speed in kilometer per hour */
127        double speedKmHour;
128
129        /**
130         * Mode
```

```
122         * A = Autonomous mode
123         * D = Differential mode
124         * E = Estimated mode
125         */
126     char mode;
127 }
128
129 /**
130 * Get latitude in degrees (decimal format)
131 */
132 double getLatitudeAsDegrees();
133 /**
134 * Get longitude in degrees (decimal format)
135 */
136 double getLongitudeAsDegrees();
137
138 /**
139 * Time, position and fix related data
140 */
141 // struct GgaType gga;
142
143 /**
144 * Course and speed information relative to ground
145 */
146 // struct VtgType vtg;
```

```
147
148
149
150
151     enum PrivConstants
152     {
153         MTK3339_BUF_SZ = 255
154     };
155
156     enum DataState
157     {
158         StateStart = 0,
159         StateData
160     };
161
162 //     char _buf[MTK3339_BUF_SZ];
163 //     int _bufPos;
164 //     enum DataState _state;
165
166     void GPS_Init( void );
167     void parseGGA( char* data , int dataLen );
168     void parseRMC( char* data , int dataLen );
169     void parseVTG( char* data , int dataLen );
170     void parseData( char* data , int len );
171     void GPS_receive( void );
```

172

173 #endif

Listing I.3: MTK3339 GPS Header File

I.4 MTK3339 GPS Source File

```
1
2  /*
3   * MTK3339.c
4   *
5   * The original C++ code has been provided by
6   * EmbeddedArtists on mbed.com
7   * https://os.mbed.com/users/embeddedartists/code/MTK3339/
8   *
9   * The following source file has been ported
10  * to C as well as modified to interact with the STM32
11  * platform.
12  *
13  * Ported and expanded on: Mar 21, 2023
14  * Author: Austin Martinez
15  */
16
17 #include "main.h"
18 #include <string.h>
19 #include <stdlib.h>
20 #include <stdio.h>
21 #include "MTK3339.h"
22
23 extern UART_HandleTypeDef huart1; // UART for GPS
```

```
24 extern UART_HandleTypeDef huart2; // UART for printing to
25   console
26 char _buf[MTK3339_BUF_SZ];
27 int _bufPos;
28 enum DataState _state;
29 struct GgaType gga;
30 struct VtgType vtg;
31 struct RmcType rmc;
32
33 void GPS_Init()
34 {
35     memset(&gga, 0, sizeof(gga));
36     memset(&vtg, 0, sizeof(vtg));
37 }
38
39 double getLatitudeAsDegrees()
40 {
41     if (gga.fix == 0 || gga.nsIndicator == 0) return 0;
42
43     double l = gga.latitude;
44     char ns = gga.nsIndicator;
45
46     // convert from ddmm.mmmm to degrees only
47     // 60 minutes is 1 degree
```

```
48
49     int deg = (int)(l / 100);
50     l = (l - deg*100.0) / 60.0;
51     l = deg + 1;
52     if (ns == 'S') l = -1;
53
54     return l;
55 }
56
57 double getLongitudeAsDegrees()
58 {
59     if (gga.fix == 0 || gga.ewIndicator == 0) return 0;
60
61     double l = gga.longitude;
62     char ew = gga.ewIndicator;
63
64     // convert from ddmm.mmmm to degrees only
65     // 60 minutes is 1 degree
66
67     int deg = (int)(l / 100);
68     l = (l - deg*100) / 60;
69     l = deg + 1;
70     if (ew == 'W') l = -1;
71
72     return l;
```

```
73  }
74
75 void parseGGA( char* data , int dataLen )
76 {
77     // http://aprs.gids.nl/nmea/#gga
78
79     double tm = 0;
80
81     memset(&gga , 0 , sizeof(gga));
82
83     char* p = data ;
84     int pos = 0;
85
86     p = strchr(p , ',' );
87     while (p != NULL && *p != 0) {
88         p++;
89
90         switch(pos) {
91             case 0: // time: hhmmss.sss
92                 tm = strtod(p , NULL);
93                 gga.hours = (int)(tm / 10000);
94                 gga.minutes = ((int)tm % 10000) / 100;
95                 gga.seconds = ((int)tm % 100);
96                 gga.milliseconds = (int)(tm * 1000) % 1000;
97                 break;
```

```
98         case 1: // latitude : ddmm.mmmm
99             gga.latitude = strtod(p, NULL);
100            gga.latitude_adj = gga.latitude / 100;
101            break;
102        case 2: // N/S indicator (north or south)
103            if (*p == 'N' || *p == 'S') {
104                gga.nsIndicator = *p;
105            }
106            break;
107        case 3: // longitude: dddmm.mmmm
108            gga.longitude = strtod(p, NULL);
109            gga.longitude_adj = gga.longitude / 100;
110            break;
111        case 4: // E/W indicator (east or west)
112            if (*p == 'E' || *p == 'W') {
113                gga.ewIndicator = *p;
114            }
115            break;
116        case 5: // position indicator (1=no fix , 2=GPS fix
117                  , 3=Differential)
118            gga.fix = strtol(p, NULL, 10);
119            break;
120        case 6: // num satellites
121            gga.satellites = strtol(p, NULL, 10);
122            break;
```

```
122         case 7: // hdop
123             gga.hdop = strtod(p, NULL);
124             break;
125         case 8: // altitude
126             gga.altitude = strtod(p, NULL);
127             break;
128         case 9: // units
129             // ignore units
130             break;
131         case 10: // geoidal separation
132             gga.geoidal = strtod(p, NULL);
133             break;
134     }
135     pos++;
136
137     p = strchr(p, ',');
138 }
139
140 }
141
142 void parseRMC(char* data, int dataLen)
143 {
144     // http://aprs.gids.nl/nmea/#gga
145
146     double tm = 0; // time
```

```
147     double dt = 0; // date
148
149     memset(&rmc, 0, sizeof(rmc));
150
151     char* p = data;
152     int pos = 0;
153
154     p = strchr(p, ',');
155     while (p != NULL && *p != 0) {
156         p++;
157
158         switch(pos) {
159             case 0: // time: hhmmss.sss
160                 tm = strtod(p, NULL);
161                 rmc.hours = (int)(tm / 10000);
162                 rmc.minutes = ((int)tm % 10000) / 100;
163                 rmc.seconds = ((int)tm % 100);
164                 rmc.milliseconds = (int)(tm * 1000) % 1000;
165                 break;
166             case 1: // status: A or V
167                 if (*p == 'A' || *p == 'V') {
168                     rmc.status = *p;
169                 }
170                 break;
171             case 2: // latitude: ddmm.mmmm
```

```
172         rmc.latitude = strtod(p, NULL);
173         break;
174     case 3: // N/S indicator (north or south)
175         if (*p == 'N' || *p == 'S') {
176             rmc.nsIndicator = *p;
177         }
178         break;
179     case 4: // longitude: dddmm.mmmm
180         rmc.longitude = strtod(p, NULL);
181         break;
182     case 5: // E/W indicator (east or west)
183         if (*p == 'E' || *p == 'W') {
184             rmc.ewIndicator = *p;
185         }
186         break;
187     case 6: // speed: z.z
188         rmc.speed = strtod(p, NULL);
189         break;
190     case 7: // course: y.y
191         rmc.course = strtod(p, NULL);
192         break;
193     case 8: // UTC date: ddmmyy
194         dt = strtod(p, NULL);
195         rmc.day = (int)(dt / 10000);
196         rmc.month = ((int)dt % 10000) / 100;
```

```
197         rmc.year = ((int)dt % 100);  
198         rmc.year = rmc.year + 2000;  
199         break;  
200     }  
201     pos++;  
202  
203     p = strchr(p, ',');  
204 }  
205  
206 }  
207  
208 void parseVTG(char* data, int dataLen)  
209 {  
210  
211  
212     char* p = data;  
213     int pos = 0;  
214  
215     memset(&vtg, 0, sizeof(vtg));  
216  
217     p = strchr(p, ',');  
218     while (p != NULL && *p != 0) {  
219         p++;  
220  
221         switch(pos) {
```

```
222         case 0: // course in degrees
223             vtg.course = strtod(p, NULL);
224             break;
225         case 1: // Reference (T)
226             break;
227         case 2: // course magnetic (need customization)
228             break;
229         case 3: // reference (M)
230             break;
231         case 4: // speed in knots
232             vtg.speedKnots = strtod(p, NULL);
233             break;
234         case 5: // units (N)
235             break;
236         case 6: // speed in Km/h
237             vtg.speedKmHour = strtod(p, NULL);
238             break;
239         case 7: // units (K)
240             break;
241         case 8: // mode
242             if ((*p == 'A' || *p == 'D' || *p == 'E')) {
243                 vtg.mode = *p;
244             }
245         break;
```

```
247
248         }
249
250         pos++;
251
252         p = strchr(p, ',');
253     }
254 }
255
256 void parseData(char* data, int len)
257 {
258     do {
259
260         // verify checksum
261         if (len < 3 || (len > 3 && data[len - 3] != '*'))
262     {
263         // invalid data
264         break;
265     }
266     int sum = strtol(&data[len - 2], NULL, 16);
267     for(int i = 1; i < len - 3; i++)
268     {
269         sum ^= data[i];
270     }
271     if (sum != 0)
```

```
272         {
273             // invalid checksum
274             break;
275         }
276
277
278         if (strncmp( "$GPGLL" , data , 6) == 0)
279     {
280             parseGLL( data , len );
281     }
282     else if (strncmp( "$GPVTG" , data , 6) == 0)
283     {
284             parseVTG( data , len );
285     }
286
287
288     } while(0);
289 }
290
291 void GPS_receive()
292 {
293     uint8_t rxByte = 0;
294     char rx_buffer[80];
295     int rx_idx = 0;
296     _Bool data_received = 0;
```

```
297     _Bool GGA_parsed = 0;
298     _Bool RMC_parsed = 0;
299
300     while (!GGA_parsed && !RMC_parsed)
301     {
302         // receive the UART data from the GPS
303         // wait until we see $GPGGA
304         if ((rx_idx < 80) && !data_received)
305         {
306             HAL_UART_Receive(&huart1, &rxByte, 1, HAL_MAX_DELAY);
307             rx_buffer[rx_idx] = rxByte;
308             if (rx_buffer[rx_idx] == '$') // beginning of some GPS
309                 output
310             {
311                 rx_idx++;
312             }
313             else if ((rx_idx > 0) && (rx_buffer[rx_idx] != '*' ||
314                     rx_buffer[rx_idx] != '\r')) // if GPS data has
315                     started AND we aren't at the end, keep collecting it
316             {
317                 rx_idx++;
318             }
319             else if (rx_buffer[rx_idx] == '*' || rx_buffer[rx_idx] ==
320                     '\r') // if we are at the end of GPS data, data has
321                     been received
```

```
317      {
318          data_received = 1;
319      }
320      else // if not beginning of GPS data ($), reset to
321          // beginning of buffer
322      {
323          rx_idx = 0;
324      }
325      // once data is received or the buffer has run out room,
326      // check if it is GGA data or RMC data
326      else
327      {
328          data_received = 0; // reset data received
329
330          if (strncmp("$GPGGA", rx_buffer, 6) == 0) // if it is
331              // GGA data
331          {
332              // char str[30] = "$GPGGA found\r\n";
333              // HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(
334                  str), HAL_MAX_DELAY);
334              parseGGA(rx_buffer, rx_idx); // if it is GGA,
335                  // parse it
335              memset(&rx_buffer, 0, sizeof(rx_buffer)); // clear
335                  // the RX buffer
```

```
336     rx_idx = 0;           // reset UART RX buffer
            index
337     GGA_parsed = 1;
338 }
339 else if (strcmp("$GPRMC", rx_buffer, 6) == 0) // if it
            is RMC data
340 {
341 //     char str[30] = "$GPRMC found\r\n";
342 //     HAL_UART_Transmit(&huart2, (uint8_t *)str, sizeof(
            str), HAL_MAX_DELAY);
343 parseRMC(rx_buffer, rx_idx);           // if it is GGA,
            parse it
344 memset(&rx_buffer, 0, sizeof(rx_buffer)); // clear
            the RX buffer
345 rx_idx = 0;           // reset UART RX buffer
            index
346 RMC_parsed = 1;
347 }
348 else
349 {
350     memset(&rx_buffer, 0, sizeof(rx_buffer)); // clear the
            RX buffer
351     rx_idx = 0; // reset UART RX buffer index
352 }
353 }
```

354 }

355 }

Listing I.4: MTK3339 GPS Source File

I.5 SPA Header File

```
1 #ifndef INC_SPA_H_
2 #define INC_SPA_H_
3
4
5
6 ///////////////////////////////////////////////////////////////////
7 //          HEADER FILE for SPA.C                //
8 //                                              //
9 //          Solar Position Algorithm (SPA)        //
10 //          for                                //
11 //          Solar Radiation Application        //
12 //                                              //
13 //          May 12, 2003                         //
14 //                                              //
15 //          Filename: SPA.H                   //
16 //                                              //
17 //          Afshin Michael Andreas            //
18 //          afshin_andreas@nrel.gov (303)384-6383 //
19 //                                              //
20 //          Measurement & Instrumentation Team   //
21 //          Solar Radiation Research Laboratory    //
22 //          National Renewable Energy Laboratory    //
23 //          1617 Cole Blvd, Golden, CO 80401      //
```

```
24 //////////////////////////////////////////////////////////////////
25
26 //
//////////////////////////////////////////////////////////////////
27 //
//
28 // Usage:
//
29 //
//
30 // 1) In calling program, include this header file,
// by adding this line to the top of file:
31 //      #include "spa.h"
//
32 //      //////////////////////////////////////////////////////////////////
33 //
//
34 // 2) In calling program, declare the SPA structure:
//
```

```
35 //           spa_data  spa;  
//  
36 //  
  
//  
37 //      3) Enter the required input values into SPA structure  
//  
38 //      (input values listed in comments below)  
//  
39 //  
  
//  
40 //      4) Call the SPA calculate function and pass the SPA  
structure      //  
41 //      (prototype is declared at the end of this header file)  
:  
//  
42 //           spa_calculate(&spa);  
//  
43 //  
  
//  
44 //      Selected output values (listed in comments below) will be  
//  
45 //      computed and returned in the passed SPA structure.  
Output      //
```

```
46 //      will based on function code selected from enumeration
        //      below.      //
47 //
//
48 //      Note: A non-zero return code from spa_calculate()
//      indicates that //
49 //      one of the input values did not pass simple bounds
//      tests.  //
50 //      The valid input ranges and return error codes are
//      also      //
51 //      listed below.
//
52 //
//
53 //
//////////////////////////////////////////////////////////////////
54
55
56 //enumeration for function codes to select desired final
//outputs from SPA
57 enum {
58     SPA_ZA,           // calculate zenith and azimuth
```

```
59     SPA_ZA_INC,           // calculate zenith , azimuth , and
          incidence
60     SPA_ZA_RTS,           // calculate zenith , azimuth , and sun
          rise / transit / set values
61     SPA_ALL,              // calculate all SPA output values
62 };
63
64 typedef struct
65 {
66     //-----INPUT VALUES
67
68     int year;                // 4-digit year ,      valid range:
          -2000 to 6000, error code: 1
69     int month;               // 2-digit month ,      valid range
          : 1 to 12,   error code: 2
70     int day;                 // 2-digit day ,       valid range
          : 1 to 31,   error code: 3
71     int hour;                // Observer local hour , valid range
          : 0 to 24,   error code: 4
72     int minute;              // Observer local minute , valid range
          : 0 to 59,   error code: 5
73     double second;           // Observer local second , valid range
          : 0 to <60,   error code: 6
74
```

```
75     double delta_ut1;      // Fractional second difference between
          UTC and UT which is used
76                           // to adjust UTC for earth's irregular
                           // rotation rate and is derived
77                           // from observation only and is
                           // reported in this bulletin:
78                           // http://maia.usno.navy.mil/ser7/ser7.
                           // dat,
79                           // where delta_ut1 = DUT1
80                           // valid range: -1 to 1 second (
                           // exclusive), error code 17
81
82     double delta_t;        // Difference between earth rotation
                           // time and terrestrial time
83                           // It is derived from observation
                           // only and is reported in this
84                           // bulletin: http://maia.usno.navy.
                           // mil/ser7/ser7.dat,
85                           // where delta_t = 32.184 + (TAI-UTC)
                           // - DUT1
86                           // valid range: -8000 to 8000 seconds
                           // , error code: 7
87
88     double timezone;       // Observer time zone (negative west
                           // of Greenwich)
```

```

89          // valid range: -18     to    18 hours ,
90                      error code: 8
91
92      double longitude;      // Observer longitude (negative west
93                      // of Greenwich)
94                      // valid range: -180   to   180 degrees
95                      , error code: 9
96
97      double latitude;       // Observer latitude (negative south
98                      // of equator)
99                      // valid range: -90    to    90 degrees
100                     , error code: 10
101
102     double elevation;      // Observer elevation [meters]
103                     // valid range: -6500000 or higher
104                     meters ,      error code: 11
105
106     double pressure;       // Annual average local pressure [
107                     millibars ]
108                     // valid range:      0 to 5000
109                     millibars ,      error code: 12
110
111     double temperature;     // Annual average local temperature [
112                     degrees Celsius ]

```

```
104           // valid range: -273 to 6000 degrees
                    Celsius , error code; 13
105
106     double slope;           // Surface slope (measured from the
                                horizontal plane)
107           // valid range: -360 to 360 degrees ,
                    error code: 14
108
109     double azm_rotation; // Surface azimuth rotation (measured
                                from south to projection of
110           //      surface normal on horizontal
                                plane , negative east)
111           // valid range: -360 to 360 degrees ,
                    error code: 15
112
113     double atmos_refract; // Atmospheric refraction at sunrise
                                and sunset (0.5667 deg is typical)
114           // valid range: -5      to      5 degrees ,
                    error code: 16
115
116     int function;          // Switch to choose functions for
                                desired output (from enumeration)
117
118 //-----Intermediate OUTPUT VALUES
-----
```

```
119
120     double jd;           // Julian day
121     double jc;           // Julian century
122
123     double jde;          // Julian ephemeris day
124     double jce;          // Julian ephemeris century
125     double jme;          // Julian ephemeris millennium
126
127     double l;             // earth heliocentric longitude [ degrees ]
128     double b;             // earth heliocentric latitude [ degrees ]
129     double r;             // earth radius vector [ Astronomical
                           Units , AU]
130
131     double theta;         // geocentric longitude [ degrees ]
132     double beta;          // geocentric latitude [ degrees ]
133
134     double x0;            // mean elongation (moon-sun) [ degrees ]
135     double x1;            // mean anomaly (sun) [ degrees ]
136     double x2;            // mean anomaly (moon) [ degrees ]
137     double x3;            // argument latitude (moon) [ degrees ]
138     double x4;            // ascending longitude (moon) [ degrees ]
139
140     double del_psi;        // nutation longitude [ degrees ]
```

```
141     double del_epsilon; // nutation obliquity [degrees]
142     double epsilon0;    // ecliptic mean obliquity [arc seconds
143             ]
144     double epsilon;      // ecliptic true obliquity [degrees]
145
146     double del_tau;     // aberration correction [degrees]
147     double lamda;       // apparent sun longitude [degrees]
148     double nu0;         // Greenwich mean sidereal time [
149             degrees]
150     double nu;          // Greenwich sidereal time [degrees]
151
152     double alpha;        // geocentric sun right ascension [
153             degrees]
154     double delta;        // geocentric sun declination [degrees]
155
156     double h;            // observer hour angle [degrees]
157     double xi;           // sun equatorial horizontal parallax [
158             degrees]
159     double del_alpha;    // sun right ascension parallax [
160             degrees]
161     double delta_prime; // topocentric sun declination [degrees
162             ]
163     double alpha_prime; // topocentric sun right ascension [
164             degrees]
```

```
158     double h_prime;           // topocentric local hour angle [
          degrees]

159     double e0;                // topocentric elevation angle (
          uncorrected) [degrees]

160     double del_e;             // atmospheric refraction correction [
          degrees]

161     double e;                 // topocentric elevation angle (
          corrected) [degrees]

162

163

164     double eot;               // equation of time [minutes]

165     double srha;              // sunrise hour angle [degrees]

166     double ssh;               // sunset hour angle [degrees]

167     double sta;               // sun transit altitude [degrees]

168

169 // -----Final OUTPUT VALUES
-----
```

170

```
171     double zenith;            // topocentric zenith angle [degrees]

172     double azimuth_astro; // topocentric azimuth angle (westward
          from south) [for astronomers]

173     double azimuth;             // topocentric azimuth angle (eastward
          from north) [for navigators and solar radiation]

174     double incidence;           // surface incidence angle [degrees]
```

175

```
176     double suntransit; // local sun transit time (or solar
177         noon) [fractional hour]
178     double sunrise; // local sunrise time (+/- 30 seconds)
179         [fractional hour]
180     double sunset; // local sunset time (+/- 30 seconds)
181         [fractional hour]
182 }
183
184 //----- Utility functions for other applications (
185 // such as NREL's SAMPA) -----
186
187 double deg2rad(double degrees);
188 double rad2deg(double radians);
189 double limit_degrees(double degrees);
190 double third_order_polynomial(double a, double b, double c,
191         double d, double x);
192
193 double geocentric_right_ascension(double lamda, double epsilon
194         , double beta);
195
196 double geocentric_declination(double beta, double epsilon ,
197         double lamda);
198
199 double observer_hour_angle(double nu, double longitude , double
200         alpha_deg);
201
202 void right_ascension_parallax_and_topocentric_dec(double
203         latitude , double elevation ,
```

```
191         double xi, double h, double delta, double *
192             delta_alpha, double *delta_prime);
193 double topocentric_right_ascension(double alpha_deg, double
194             delta_alpha);
195 double topocentric_local_hour_angle(double h, double
196             delta_alpha);
197 double topocentric_elevation_angle(double latitude, double
198             delta_prime, double h_prime);
199 double atmospheric_refraction_correction(double pressure,
200             double temperature,
201                                         double atmos_refract,
202                                         double e0);
203 double topocentric_elevation_angle_corrected(double e0, double
204             delta_e);
205 double topocentric_zenith_angle(double e);
206 double topocentric_azimuth_angle_astro(double h_prime, double
207             latitude, double delta_prime);
208 double topocentric_azimuth_angle(double azimuth_astro);
209
210
211 // Calculate SPA output values (in structure) based on input
212 // values passed in structure
213 int spa_calculate(spa_data *spa);
214
215
216
```

```
207 #endif /* INC_SPA_H_ */
```

Listing I.5: SPA Header File

I.6 SPA Source File

```
1 //////////////////////////////////////////////////////////////////
2 // Solar Position Algorithm (SPA) //
3 // for //
4 // Solar Radiation Application //
5 // //
6 // May 12, 2003 //
7 // //
8 // Filename: SPA.C //
9 // //
10 // Afshin Michael Andreas //
11 // Afshin.Andreas@NREL.gov (303)384-6383 //
12 // //
13 // Metrology Laboratory //
14 // Solar Radiation Research Laboratory //
15 // National Renewable Energy Laboratory //
16 // 15013 Denver W Pkwy, Golden, CO 80401 //
17 //////////////////////////////////////////////////////////////////
18
19 //////////////////////////////////////////////////////////////////
20 // See the SPA.H header file for usage //
21 // //
22 // This code is based on the NREL //
23 // technical report "Solar Position //
```

```
24 //      Algorithm for Solar Radiation          //
25 //      Application" by I. Reda & A. Andreas  //
26 ///////////////////////////////////////////////////////////////////
27
28 //
///////////////////////////////////////////////////////////////////
29 //
30 //      NOTICE
31 //      Copyright (C) 2008–2011 Alliance for Sustainable Energy,
32 //      LLC, All Rights Reserved
33 //The Solar Position Algorithm ("Software") is code in
34 //development prepared by employees of the
35 //Alliance for Sustainable Energy, LLC, (hereinafter the "
36 //Contractor"), under Contract No.
37 //DE-AC36-08GO28308 ("Contract") with the U.S. Department of
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43 //works, and perform publicly and display publicly. Beginning
44 //five (5) years after the date
```

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Contractor ceases to make this
44 // computer software available, it may be obtained from DOE's
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49 // U.S. GOVERNMENT BE LIABLE FOR ANY SPECIAL, INDIRECT OR
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50 // WHATSOEVER, INCLUDING BUT NOT LIMITED TO CLAIMS ASSOCIATED
WITH THE LOSS OF DATA OR PROFITS,

51 //WHICH MAY RESULT FROM AN ACTION IN CONTRACT, NEGLIGENCE OR
OTHER TORTIOUS CLAIM THAT ARISES

52 //OUT OF OR IN CONNECTION WITH THE ACCESS, USE OR PERFORMANCE
OF THIS SOFTWARE.

53 //

54 //The Software is being provided for internal, noncommercial
purposes only and shall not be

55 //re-distributed. Please contact the NREL Commercialization
and Technology Transfer Office

56 //for information concerning a commercial license to use the
Software, visit:

57 // <http://midcdmz.nrel.gov/spa/> for the contact information.

58 //

59 //As a condition of using the Software in an application, the
developer of the application

60 //agrees to reference the use of the Software and make this
Notice readily accessible to any

61 //end-user in a Help|About screen or equivalent manner.

62 //

63 //

//////////

64

65 //

//////////

```
66 // Revised 27-FEB-2004 Andreas
67 //           Added bounds check on inputs and return value for
    spa_calculate().
68 // Revised 10-MAY-2004 Andreas
69 //           Changed temperature bound check minimum from
    -273.15 to -273 degrees C.
70 // Revised 17-JUN-2004 Andreas
71 //           Corrected a problem that caused a bogus sunrise/set
    / transit on the equinox.
72 // Revised 18-JUN-2004 Andreas
73 //           Added a "function" input variable that allows the
    selecting of desired outputs.
74 // Revised 21-JUN-2004 Andreas
75 //           Added 3 new intermediate output values to SPA
    structure (srha, ssh, & sta).
76 // Revised 23-JUN-2004 Andreas
77 //           Enumerations for "function" were renamed and 2 were
    added.
78 //           Prevented bound checks on inputs that are not used
    (based on function).
79 // Revised 01-SEP-2004 Andreas
80 //           Changed a local variable from integer to double.
81 // Revised 12-JUL-2005 Andreas
```

```
82 // Put a limit on the EOT calculation , so that the
     result is between -20 and 20.
83 // Revised 26-OCT-2005 Andreas
84 // Set the atmos. refraction correction to zero , when
     sun is below horizon .
85 // Made atmos_refract input a requirement for all "
     functions ".
86 // Changed atmos_refract bound check from +/- 10 to
     +/- 5 degrees .
87 // Revised 07-NOV-2006 Andreas
88 // Corrected 3 earth periodic terms in the L_TERMS
     array .
89 // Corrected 2 earth periodic terms in the R_TERMS
     array .
90 // Revised 10-NOV-2006 Andreas
91 // Corrected a constant used to calculate topocentric
     sun declination .
92 // Put a limit on observer hour angle , so result is
     between 0 and 360.
93 // Revised 13-NOV-2006 Andreas
94 // Corrected calculation of topocentric sun
     declination .
95 // Converted all floating point inputs in spa
     structure to doubles .
96 // Revised 27-FEB-2007 Andreas
```

```
97 //           Minor correction made as to when atmos. refraction
      correction is set to zero.

98 // Revised 21-JAN-2008 Andreas

99 //           Minor change to two variable declarations.

100 // Revised 12-JAN-2009 Andreas

101 //           Changed timezone bound check from +/-12 to +/-18
      hours.

102 // Revised 14-JAN-2009 Andreas

103 //           Corrected a constant used to calculate ecliptic
      mean obliquity.

104 // Revised 01-APR-2013 Andreas

105 //           Replace floor with new integer function for tech.
      report consistency, no affect on results.

106 //           Add "utility" function prototypes to header file
      for use with NREL's SAMPA.

107 //           Rename 4 "utility" function names (remove "sun")
      for clarity with NREL's SAMPA.

108 //           Added delta_ut1 as required input, which the
      fractional second difference between UT and UTC.

109 //           Time must be input w/o delta_ut1 adjustment,
      instead of assuming adjustment was pre-applied.

110 // Revised 10-JUL-2014 Andreas

111 //           Change second in spa_data structure from an integer
      to double to allow fractional second

112 // Revised 08-SEP-2014 Andreas
```

```
113 //           Corrected description of azm_rotation in header
      file
114 //           Limited azimuth180 to range of 0 to 360 deg (
      instead of -180 to 180) for tech report consistency
115 //           Changed all variables names from azimuth180 to
      azimuth_astro
116 //           Renamed 2 "utility" function names for consistency
117 //
      /////////////////////////////////
118
119 #include <math.h>
120 #include "spa.h"
121
122 #define PI           3.1415926535897932384626433832795028841971
123 #define SUN_RADIUS 0.26667
124
125 #define L_COUNT 6
126 #define B_COUNT 2
127 #define R_COUNT 5
128 #define Y_COUNT 63
129
130 #define L_MAX_SUBCOUNT 64
131 #define B_MAX_SUBCOUNT 5
132 #define R_MAX_SUBCOUNT 40
```

```
133
134 enum {TERM_A, TERM_B, TERM_C, TERM_COUNT};
135 enum {TERM_X0, TERM_X1, TERM_X2, TERM_X3, TERM_X4,
136 TERM_X_COUNT};
137 enum {JD_MINUS, JD_ZERO, JD_PLUS, JD_COUNT};
138 enum {SUN_TRANSIT, SUN_RISE, SUN_SET, SUN_COUNT};
139
140 #define TERM_Y_COUNT TERM_X_COUNT
141
142 const int l_subcount[L_COUNT] = {64,34,20,7,3,1};
143 const int b_subcount[B_COUNT] = {5,2};
144 const int r_subcount[R_COUNT] = {40,10,6,2,1};
145
146 ///////////////////////////////////////////////////////////////////
147 /// Earth Periodic Terms
148 ///////////////////////////////////////////////////////////////////
149 const double L_TERMS[L_COUNT][L_MAX_SUBCOUNT][TERM_COUNT]=
150 {
151     {
152         {175347046.0,0,0},
153         {3341656.0,4.6692568,6283.07585},
154         {34894.0,4.6261,12566.1517},
155         {3497.0,2.7441,5753.3849},
```

```
156     {3418.0,2.8289,3.5231},  
157     {3136.0,3.6277,77713.7715},  
158     {2676.0,4.4181,7860.4194},  
159     {2343.0,6.1352,3930.2097},  
160     {1324.0,0.7425,11506.7698},  
161     {1273.0,2.0371,529.691},  
162     {1199.0,1.1096,1577.3435},  
163     {990,5.233,5884.927},  
164     {902,2.045,26.298},  
165     {857,3.508,398.149},  
166     {780,1.179,5223.694},  
167     {753,2.533,5507.553},  
168     {505,4.583,18849.228},  
169     {492,4.205,775.523},  
170     {357,2.92,0.067},  
171     {317,5.849,11790.629},  
172     {284,1.899,796.298},  
173     {271,0.315,10977.079},  
174     {243,0.345,5486.778},  
175     {206,4.806,2544.314},  
176     {205,1.869,5573.143},  
177     {202,2.458,6069.777},  
178     {156,0.833,213.299},  
179     {132,3.411,2942.463},  
180     {126,1.083,20.775},
```

```
181      { 115 ,0.645 ,0.98 } ,  
182      { 103 ,0.636 ,4694.003 } ,  
183      { 102 ,0.976 ,15720.839 } ,  
184      { 102 ,4.267 ,7.114 } ,  
185      { 99 ,6.21 ,2146.17 } ,  
186      { 98 ,0.68 ,155.42 } ,  
187      { 86 ,5.98 ,161000.69 } ,  
188      { 85 ,1.3 ,6275.96 } ,  
189      { 85 ,3.67 ,71430.7 } ,  
190      { 80 ,1.81 ,17260.15 } ,  
191      { 79 ,3.04 ,12036.46 } ,  
192      { 75 ,1.76 ,5088.63 } ,  
193      { 74 ,3.5 ,3154.69 } ,  
194      { 74 ,4.68 ,801.82 } ,  
195      { 70 ,0.83 ,9437.76 } ,  
196      { 62 ,3.98 ,8827.39 } ,  
197      { 61 ,1.82 ,7084.9 } ,  
198      { 57 ,2.78 ,6286.6 } ,  
199      { 56 ,4.39 ,14143.5 } ,  
200      { 56 ,3.47 ,6279.55 } ,  
201      { 52 ,0.19 ,12139.55 } ,  
202      { 52 ,1.33 ,1748.02 } ,  
203      { 51 ,0.28 ,5856.48 } ,  
204      { 49 ,0.49 ,1194.45 } ,  
205      { 41 ,5.37 ,8429.24 } ,
```

```
206      { 41 , 2.4 , 19651.05 } ,  
207      { 39 , 6.17 , 10447.39 } ,  
208      { 37 , 6.04 , 10213.29 } ,  
209      { 37 , 2.57 , 1059.38 } ,  
210      { 36 , 1.71 , 2352.87 } ,  
211      { 36 , 1.78 , 6812.77 } ,  
212      { 33 , 0.59 , 17789.85 } ,  
213      { 30 , 0.44 , 83996.85 } ,  
214      { 30 , 2.74 , 1349.87 } ,  
215      { 25 , 3.16 , 4690.48 }  
216      } ,  
217      {  
218      { 628331966747.0 , 0 , 0 } ,  
219      { 206059.0 , 2.678235 , 6283.07585 } ,  
220      { 4303.0 , 2.6351 , 12566.1517 } ,  
221      { 425.0 , 1.59 , 3.523 } ,  
222      { 119.0 , 5.796 , 26.298 } ,  
223      { 109.0 , 2.966 , 1577.344 } ,  
224      { 93 , 2.59 , 18849.23 } ,  
225      { 72 , 1.14 , 529.69 } ,  
226      { 68 , 1.87 , 398.15 } ,  
227      { 67 , 4.41 , 5507.55 } ,  
228      { 59 , 2.89 , 5223.69 } ,  
229      { 56 , 2.17 , 155.42 } ,  
230      { 45 , 0.4 , 796.3 } ,
```

```
231      { 36 ,0.47 ,775.52 } ,  
232      { 29 ,2.65 ,7.11 } ,  
233      { 21 ,5.34 ,0.98 } ,  
234      { 19 ,1.85 ,5486.78 } ,  
235      { 19 ,4.97 ,213.3 } ,  
236      { 17 ,2.99 ,6275.96 } ,  
237      { 16 ,0.03 ,2544.31 } ,  
238      { 16 ,1.43 ,2146.17 } ,  
239      { 15 ,1.21 ,10977.08 } ,  
240      { 12 ,2.83 ,1748.02 } ,  
241      { 12 ,3.26 ,5088.63 } ,  
242      { 12 ,5.27 ,1194.45 } ,  
243      { 12 ,2.08 ,4694 } ,  
244      { 11 ,0.77 ,553.57 } ,  
245      { 10 ,1.3 ,6286.6 } ,  
246      { 10 ,4.24 ,1349.87 } ,  
247      { 9 ,2.7 ,242.73 } ,  
248      { 9 ,5.64 ,951.72 } ,  
249      { 8 ,5.3 ,2352.87 } ,  
250      { 6 ,2.65 ,9437.76 } ,  
251      { 6 ,4.67 ,4690.48 }  
252      },  
253      {  
254      { 52919.0 ,0 ,0 } ,  
255      { 8720.0 ,1.0721 ,6283.0758 } ,
```

```
256     { 309.0 ,0.867 ,12566.152 } ,  
257     { 27 ,0.05 ,3.52 } ,  
258     { 16 ,5.19 ,26.3 } ,  
259     { 16 ,3.68 ,155.42 } ,  
260     { 10 ,0.76 ,18849.23 } ,  
261     { 9 ,2.06 ,77713.77 } ,  
262     { 7 ,0.83 ,775.52 } ,  
263     { 5 ,4.66 ,1577.34 } ,  
264     { 4 ,1.03 ,7.11 } ,  
265     { 4 ,3.44 ,5573.14 } ,  
266     { 3 ,5.14 ,796.3 } ,  
267     { 3 ,6.05 ,5507.55 } ,  
268     { 3 ,1.19 ,242.73 } ,  
269     { 3 ,6.12 ,529.69 } ,  
270     { 3 ,0.31 ,398.15 } ,  
271     { 3 ,2.28 ,553.57 } ,  
272     { 2 ,4.38 ,5223.69 } ,  
273     { 2 ,3.75 ,0.98 }  
274 },  
275 {  
276     { 289.0 ,5.844 ,6283.076 } ,  
277     { 35 ,0 ,0 } ,  
278     { 17 ,5.49 ,12566.15 } ,  
279     { 3 ,5.2 ,155.42 } ,  
280     { 1 ,4.72 ,3.52 } ,
```

```
281         { 1 ,5.3 ,18849.23 } ,
282         { 1 ,5.97 ,242.73 }
283     },
284     {
285         { 114.0 ,3.142 ,0 } ,
286         { 8 ,4.13 ,6283.08 } ,
287         { 1 ,3.84 ,12566.15 }
288     },
289     {
290         { 1 ,3.14 ,0 }
291     }
292 };
293
294 const double B_TERMS[B_COUNT][B_MAX_SUBCOUNT][TERM_COUNT]=
295 {
296     {
297         { 280.0 ,3.199 ,84334.662 } ,
298         { 102.0 ,5.422 ,5507.553 } ,
299         { 80 ,3.88 ,5223.69 } ,
300         { 44 ,3.7 ,2352.87 } ,
301         { 32 ,4 ,1577.34 }
302     },
303     {
304         { 9 ,3.9 ,5507.55 } ,
305         { 6 ,1.73 ,5223.69 }
```

```
306      }
307  };
308
309 const double R_TERMS[R_COUNT][R_MAX_SUBCOUNT][TERM_COUNT]=
310 {
311   {
312     {100013989.0,0,0},
313     {1670700.0,3.0984635,6283.07585},
314     {13956.0,3.05525,12566.1517},
315     {3084.0,5.1985,77713.7715},
316     {1628.0,1.1739,5753.3849},
317     {1576.0,2.8469,7860.4194},
318     {925.0,5.453,11506.77},
319     {542.0,4.564,3930.21},
320     {472.0,3.661,5884.927},
321     {346.0,0.964,5507.553},
322     {329.0,5.9,5223.694},
323     {307.0,0.299,5573.143},
324     {243.0,4.273,11790.629},
325     {212.0,5.847,1577.344},
326     {186.0,5.022,10977.079},
327     {175.0,3.012,18849.228},
328     {110.0,5.055,5486.778},
329     {98,0.89,6069.78},
330     {86,5.69,15720.84},
```

```
331     { 86 ,1.27 ,161000.69 } ,  
332     { 65 ,0.27 ,17260.15 } ,  
333     { 63 ,0.92 ,529.69 } ,  
334     { 57 ,2.01 ,83996.85 } ,  
335     { 56 ,5.24 ,71430.7 } ,  
336     { 49 ,3.25 ,2544.31 } ,  
337     { 47 ,2.58 ,775.52 } ,  
338     { 45 ,5.54 ,9437.76 } ,  
339     { 43 ,6.01 ,6275.96 } ,  
340     { 39 ,5.36 ,4694 } ,  
341     { 38 ,2.39 ,8827.39 } ,  
342     { 37 ,0.83 ,19651.05 } ,  
343     { 37 ,4.9 ,12139.55 } ,  
344     { 36 ,1.67 ,12036.46 } ,  
345     { 35 ,1.84 ,2942.46 } ,  
346     { 33 ,0.24 ,7084.9 } ,  
347     { 32 ,0.18 ,5088.63 } ,  
348     { 32 ,1.78 ,398.15 } ,  
349     { 28 ,1.21 ,6286.6 } ,  
350     { 28 ,1.9 ,6279.55 } ,  
351     { 26 ,4.59 ,10447.39 }  
352 },  
353 {  
354     { 103019.0 ,1.10749 ,6283.07585 } ,  
355     { 1721.0 ,1.0644 ,12566.1517 } ,
```

```
356     { 702.0 , 3.142 , 0 } ,  
357     { 32 , 1.02 , 18849.23 } ,  
358     { 31 , 2.84 , 5507.55 } ,  
359     { 25 , 1.32 , 5223.69 } ,  
360     { 18 , 1.42 , 1577.34 } ,  
361     { 10 , 5.91 , 10977.08 } ,  
362     { 9 , 1.42 , 6275.96 } ,  
363     { 9 , 0.27 , 5486.78 }  
364 },  
365 {  
366     { 4359.0 , 5.7846 , 6283.0758 } ,  
367     { 124.0 , 5.579 , 12566.152 } ,  
368     { 12 , 3.14 , 0 } ,  
369     { 9 , 3.63 , 77713.77 } ,  
370     { 6 , 1.87 , 5573.14 } ,  
371     { 3 , 5.47 , 18849.23 }  
372 },  
373 {  
374     { 145.0 , 4.273 , 6283.076 } ,  
375     { 7 , 3.92 , 12566.15 }  
376 },  
377 {  
378     { 4 , 2.56 , 6283.08 }  
379 }  
380 };
```

381

382 //

//////////

383 /// Periodic Terms for the nutation in longitude and
obliquity

384 //

//////////

385

386 const int Y_TERMS[Y_COUNT][TERM_Y_COUNT]=

387 {

388 {0,0,0,0,1},

389 {-2,0,0,2,2},

390 {0,0,0,2,2},

391 {0,0,0,0,2},

392 {0,1,0,0,0},

393 {0,0,1,0,0},

394 {-2,1,0,2,2},

395 {0,0,0,2,1},

396 {0,0,1,2,2},

397 {-2,-1,0,2,2},

398 {-2,0,1,0,0},

399 {-2,0,0,2,1},

400 {0,0,-1,2,2},

```
401      { 2 ,0 ,0 ,0 ,0 } ,  
402      { 0 ,0 ,1 ,0 ,1 } ,  
403      { 2 ,0 ,-1 ,2 ,2 } ,  
404      { 0 ,0 ,-1 ,0 ,1 } ,  
405      { 0 ,0 ,1 ,2 ,1 } ,  
406      { -2 ,0 ,2 ,0 ,0 } ,  
407      { 0 ,0 ,-2 ,2 ,1 } ,  
408      { 2 ,0 ,0 ,2 ,2 } ,  
409      { 0 ,0 ,2 ,2 ,2 } ,  
410      { 0 ,0 ,2 ,0 ,0 } ,  
411      { -2 ,0 ,1 ,2 ,2 } ,  
412      { 0 ,0 ,0 ,2 ,0 } ,  
413      { -2 ,0 ,0 ,2 ,0 } ,  
414      { 0 ,0 ,-1 ,2 ,1 } ,  
415      { 0 ,2 ,0 ,0 ,0 } ,  
416      { 2 ,0 ,-1 ,0 ,1 } ,  
417      { -2 ,2 ,0 ,2 ,2 } ,  
418      { 0 ,1 ,0 ,0 ,1 } ,  
419      { -2 ,0 ,1 ,0 ,1 } ,  
420      { 0 ,-1 ,0 ,0 ,1 } ,  
421      { 0 ,0 ,2 ,-2 ,0 } ,  
422      { 2 ,0 ,-1 ,2 ,1 } ,  
423      { 2 ,0 ,1 ,2 ,2 } ,  
424      { 0 ,1 ,0 ,2 ,2 } ,  
425      { -2 ,1 ,1 ,0 ,0 } ,
```

```
426      { 0 ,-1 ,0 ,2 ,2 } ,  
427      { 2 ,0 ,0 ,2 ,1 } ,  
428      { 2 ,0 ,1 ,0 ,0 } ,  
429      { -2 ,0 ,2 ,2 ,2 } ,  
430      { -2 ,0 ,1 ,2 ,1 } ,  
431      { 2 ,0 ,-2 ,0 ,1 } ,  
432      { 2 ,0 ,0 ,0 ,1 } ,  
433      { 0 ,-1 ,1 ,0 ,0 } ,  
434      { -2 ,-1 ,0 ,2 ,1 } ,  
435      { -2 ,0 ,0 ,0 ,1 } ,  
436      { 0 ,0 ,2 ,2 ,1 } ,  
437      { -2 ,0 ,2 ,0 ,1 } ,  
438      { -2 ,1 ,0 ,2 ,1 } ,  
439      { 0 ,0 ,1 ,-2 ,0 } ,  
440      { -1 ,0 ,1 ,0 ,0 } ,  
441      { -2 ,1 ,0 ,0 ,0 } ,  
442      { 1 ,0 ,0 ,0 ,0 } ,  
443      { 0 ,0 ,1 ,2 ,0 } ,  
444      { 0 ,0 ,-2 ,2 ,2 } ,  
445      { -1 ,-1 ,1 ,0 ,0 } ,  
446      { 0 ,1 ,1 ,0 ,0 } ,  
447      { 0 ,-1 ,1 ,2 ,2 } ,  
448      { 2 ,-1 ,-1 ,2 ,2 } ,  
449      { 0 ,0 ,3 ,2 ,2 } ,  
450      { 2 ,-1 ,0 ,2 ,2 } ,
```

```
451  };
452
453 const double PE_TERMS[Y_COUNT][TERM_PE_COUNT]={
454     { -171996,-174.2,92025,8.9} ,
455     { -13187,-1.6,5736,-3.1} ,
456     { -2274,-0.2,977,-0.5} ,
457     { 2062,0.2,-895,0.5} ,
458     { 1426,-3.4,54,-0.1} ,
459     { 712,0.1,-7,0} ,
460     { -517,1.2,224,-0.6} ,
461     { -386,-0.4,200,0} ,
462     { -301,0,129,-0.1} ,
463     { 217,-0.5,-95,0.3} ,
464     { -158,0,0,0} ,
465     { 129,0.1,-70,0} ,
466     { 123,0,-53,0} ,
467     { 63,0,0,0} ,
468     { 63,0.1,-33,0} ,
469     { -59,0,26,0} ,
470     { -58,-0.1,32,0} ,
471     { -51,0,27,0} ,
472     { 48,0,0,0} ,
473     { 46,0,-24,0} ,
474     { -38,0,16,0} ,
475     { -31,0,13,0} ,
```

```
476      { 29 ,0 ,0 ,0 } ,  
477      { 29 ,0 ,-12 ,0 } ,  
478      { 26 ,0 ,0 ,0 } ,  
479      { -22 ,0 ,0 ,0 } ,  
480      { 21 ,0 ,-10 ,0 } ,  
481      { 17 ,-0.1 ,0 ,0 } ,  
482      { 16 ,0 ,-8 ,0 } ,  
483      { -16 ,0.1 ,7 ,0 } ,  
484      { -15 ,0 ,9 ,0 } ,  
485      { -13 ,0 ,7 ,0 } ,  
486      { -12 ,0 ,6 ,0 } ,  
487      { 11 ,0 ,0 ,0 } ,  
488      { -10 ,0 ,5 ,0 } ,  
489      { -8 ,0 ,3 ,0 } ,  
490      { 7 ,0 ,-3 ,0 } ,  
491      { -7 ,0 ,0 ,0 } ,  
492      { -7 ,0 ,3 ,0 } ,  
493      { -7 ,0 ,3 ,0 } ,  
494      { 6 ,0 ,0 ,0 } ,  
495      { 6 ,0 ,-3 ,0 } ,  
496      { 6 ,0 ,-3 ,0 } ,  
497      { -6 ,0 ,3 ,0 } ,  
498      { -6 ,0 ,3 ,0 } ,  
499      { 5 ,0 ,0 ,0 } ,  
500      { -5 ,0 ,3 ,0 } ,
```

```
501      { -5 ,0 ,3 ,0 } ,  
502      { -5 ,0 ,3 ,0 } ,  
503      { 4 ,0 ,0 ,0 } ,  
504      { 4 ,0 ,0 ,0 } ,  
505      { 4 ,0 ,0 ,0 } ,  
506      { -4 ,0 ,0 ,0 } ,  
507      { -4 ,0 ,0 ,0 } ,  
508      { -4 ,0 ,0 ,0 } ,  
509      { 3 ,0 ,0 ,0 } ,  
510      { -3 ,0 ,0 ,0 } ,  
511      { -3 ,0 ,0 ,0 } ,  
512      { -3 ,0 ,0 ,0 } ,  
513      { -3 ,0 ,0 ,0 } ,  
514      { -3 ,0 ,0 ,0 } ,  
515      { -3 ,0 ,0 ,0 } ,  
516      { -3 ,0 ,0 ,0 } ,  
517  };  
518  
519 ///////////////////////////////////////////////////////////////////  
520  
521 double rad2deg( double radians )  
522 {  
523     return (180.0/PI)*radians ;  
524 }  
525
```

```
526 double deg2rad(double degrees)
527 {
528     return (PI/180.0)*degrees;
529 }
530
531 int integer(double value)
532 {
533     return value;
534 }
535
536 double limit_degrees(double degrees)
537 {
538     double limited;
539
540     degrees /= 360.0;
541     limited = 360.0*(degrees-floor(degrees));
542     if (limited < 0) limited += 360.0;
543
544     return limited;
545 }
546
547 double limit_degrees180pm(double degrees)
548 {
549     double limited;
```

```
551     degrees /= 360.0;
552     limited = 360.0*(degrees-floor(degrees));
553     if       (limited < -180.0) limited += 360.0;
554     else if (limited > 180.0) limited -= 360.0;
555
556     return limited;
557 }
558
559 double limit_degrees180(double degrees)
560 {
561     double limited;
562
563     degrees /= 180.0;
564     limited = 180.0*(degrees-floor(degrees));
565     if (limited < 0) limited += 180.0;
566
567     return limited;
568 }
569
570 double limit_zero2one(double value)
571 {
572     double limited;
573
574     limited = value - floor(value);
575     if (limited < 0) limited += 1.0;
```

```
576
577     return limited;
578 }
579
580 double limit_minutes(double minutes)
581 {
582     double limited=minutes;
583
584     if (limited < -20.0) limited += 1440.0;
585     else if (limited > 20.0) limited -= 1440.0;
586
587     return limited;
588 }
589
590 double dayfrac_to_local_hr(double dayfrac, double timezone)
591 {
592     return 24.0*limit_zeroZone(dayfrac + timezone/24.0);
593 }
594
595 double third_order_polynomial(double a, double b, double c,
596                                 double d, double x)
597 {
598     return ((a*x + b)*x + c)*x + d;
599 }
```

```
600 //
```

```
////////////////////////////////////////////////////////////////
```

```
601 int validate_inputs(spa_data *spa)
602 {
603     if ((spa->year < -2000) || (spa->year >
604         6000)) return 1;
604     if ((spa->month < 1) || (spa->month > 12
605 )) return 2;
605     if ((spa->day < 1) || (spa->day > 31
606 )) return 3;
606     if ((spa->hour < 0) || (spa->hour > 24
607 )) return 4;
607     if ((spa->minute < 0) || (spa->minute > 59
608 )) return 5;
608     if ((spa->second < 0) || (spa->second >=60
609 )) return 6;
609     if ((spa->pressure < 0) || (spa->pressure >
610         5000)) return 12;
610     if ((spa->temperature <= -273) || (spa->temperature >
611         6000)) return 13;
611     if ((spa->delta_ut1 <= -1) || (spa->delta_ut1 >= 1
612 )) return 17;
612     if ((spa->hour == 24) && (spa->minute > 0))
613         return 5;
```

```
613     if ((spa->hour == 24) && (spa->second > 0
614         )) return 6;
615
616     if (fabs(spa->delta_t) > 8000) return 7;
617     if (fabs(spa->timezone) > 18) return 8;
618     if (fabs(spa->longitude) > 180) return 9;
619     if (fabs(spa->latitude) > 90) return 10;
620     if (fabs(spa->atmos_refract) > 5) return 16;
621     if (spa->elevation < -6500000) return 11;
622
623     if ((spa->function == SPA_ZA_INC) || (spa->function ==
624         SPA_ALL))
625     {
626         if (fabs(spa->slope) > 360) return 14;
627         if (fabs(spa->azm_rotation) > 360) return 15;
628     }
629
630 //////////////////////////////////////////////////////////////////
631 double julian_day (int year, int month, int day, int hour, int
632 minute, double second, double dut1, double tz)
633 {
```

```
633     double day_decimal, julian_day, a;
634
635     day_decimal = day + (hour - tz + (minute + (second + dut1)
636                           /60.0)/60.0)/24.0;
637
638     if (month < 3) {
639         month += 12;
640         year--;
641     }
642
643     julian_day = integer(365.25*(year+4716.0)) + integer
644             (30.6001*(month+1)) + day_decimal - 1524.5;
645
646     if (julian_day > 2299160.0) {
647         a = integer(year/100);
648         julian_day += (2 - a + integer(a/4));
649     }
650
651
652     return julian_day;
653 }
654
655 }
```

```
656
657 double julian_ephemeris_day(double jd, double delta_t)
658 {
659     return jd+delta_t/86400.0;
660 }
661
662 double julian_ephemeris_century(double jde)
663 {
664     return (jde - 2451545.0)/36525.0;
665 }
666
667 double julian_ephemeris_millennium(double jce)
668 {
669     return (jce/10.0);
670 }
671
672 double earth_periodic_term_summation(const double terms[] [
    TERM_COUNT], int count, double jme)
673 {
674     int i;
675     double sum=0;
676
677     for (i = 0; i < count; i++)
678         sum += terms[i][TERM_A]*cos(terms[i][TERM_B]+terms[i][
    TERM_C])*jme);
```



```
703
704     return limit_degrees(rad2deg(earth_values(sum, L_COUNT,
705                               jme)));
706 }
707
708 double earth_heliocentric_latitude(double jme)
709 {
710     double sum[B_COUNT];
711     int i;
712
713     for (i = 0; i < B_COUNT; i++)
714         sum[i] = earth_periodic_term_summation(B_TERMS[i],
715                                               b_subcount[i], jme);
716
717     return rad2deg(earth_values(sum, B_COUNT, jme));
718 }
719
720 double earth_radius_vector(double jme)
721 {
722     double sum[R_COUNT];
723     int i;
724
725     for (i = 0; i < R_COUNT; i++)
```

```
726     sum[ i ] = earth_periodic_term_summation(R_TERMS[ i ] ,  
727         r_subcount[ i ] , jme);  
728  
729     return earth_values(sum, R_COUNT, jme);  
730 }  
731  
732 double geocentric_longitude(double l)  
733 {  
734     double theta = l + 180.0;  
735  
736     if (theta >= 360.0) theta -= 360.0;  
737  
738     return theta;  
739 }  
740  
741 double geocentric_latitude(double b)  
742 {  
743     return -b;  
744 }  
745  
746 double mean_elongation_moon_sun(double jce)  
747 {  
748     return third_order_polynomial(1.0/189474.0, -0.0019142,  
        445267.11148, 297.85036, jce);
```

```
749 }
750
751 double mean_anomaly_sun(double jce)
752 {
753     return third_order_polynomial(-1.0/300000.0, -0.0001603,
754         35999.05034, 357.52772, jce);
755
756 double mean_anomaly_moon(double jce)
757 {
758     return third_order_polynomial(1.0/56250.0, 0.0086972,
759         477198.867398, 134.96298, jce);
760
761 double argument_latitude_moon(double jce)
762 {
763     return third_order_polynomial(1.0/327270.0, -0.0036825,
764         483202.017538, 93.27191, jce);
765
766 double ascending_longitude_moon(double jce)
767 {
768     return third_order_polynomial(1.0/450000.0, 0.0020708,
769         -1934.136261, 125.04452, jce);
```

```
770
771 double xy_term_summation( int i , double x[TERM_X_COUNT])
772 {
773     int j ;
774     double sum=0;
775
776     for (j = 0; j < TERM_Y_COUNT; j++)
777         sum += x[j]*Y_TERMS[ i ][ j ];
778
779     return sum;
780 }
781
782 void nutation_longitude_and_obliquity( double jce , double x[
783 TERM_X_COUNT] , double *del_psi ,
784
785     double *del_epsilon )
786 {
787     int i ;
788     double xy_term_sum , sum_psi=0, sum_epsilon=0;
789
790     for (i = 0; i < Y_COUNT; i++) {
791         xy_term_sum = deg2rad( xy_term_summation(i , x));
792         sum_psi      += (PE_TERMS[ i ][ TERM_PSI_A ] + jce *PE_TERMS
793
794             [ i ][ TERM_PSI_B ]) * sin( xy_term_sum );
795         sum_epsilon += (PE_TERMS[ i ][ TERM_EPS_C ] + jce *PE_TERMS
796
797             [ i ][ TERM_EPS_D ]) * cos( xy_term_sum );
```

```
792      }
793
794      *del_psi      = sum_psi      / 36000000.0;
795      *del_epsilon = sum_epsilon / 36000000.0;
796  }
797
798 double ecliptic_mean_obliquity(double jme)
799 {
800     double u = jme/10.0;
801
802     return 84381.448 + u*(-4680.93 + u*(-1.55 + u*(1999.25 + u
803                                     *(-51.38 + u*(-249.67 +
804                                     u*(- -39.05 + u*( 7.12 + u*( 27.87 + u
805                                     *( 5.79 + u*2.45))))))) );
806
807  }
808
809 double ecliptic_true_obliquity(double delta_epsilon , double
810 epsilon0)
811
812 {
813     return delta_epsilon + epsilon0/3600.0;
814
815
816 double aberration_correction(double r)
817 {
818     return -20.4898 / (3600.0*r);
```

```
814  }
815
816 double apparent_sun_longitude(double theta, double delta_psi,
817   double delta_tau)
817 {
818     return theta + delta_psi + delta_tau;
819 }
820
821 double greenwich_mean_sidereal_time (double jd, double jc)
822 {
823     return limit_degrees(280.46061837 + 360.98564736629 * (jd
824           - 2451545.0) +
824           jc*jc *(0.000387933 - jc
824           /38710000.0));
825 }
826
827 double greenwich_sidereal_time (double nu0, double delta_psi,
828   double epsilon)
828 {
829     return nu0 + delta_psi*cos(deg2rad(epsilon));
830 }
831
832 double geocentric_right_ascension(double lamda, double epsilon
833   , double beta)
833 {
```

```
834     double lamda_rad    = deg2rad(lamda);  
835     double epsilon_rad = deg2rad(epsilon);  
836  
837     return limit_degrees(rad2deg(atan2(sin(lamda_rad)*cos(  
838                     tan(deg2rad(beta))*sin(epsilon_rad), cos(  
839                     lamda_rad))));  
840  
841 double geocentric_declination(double beta, double epsilon,  
842     double lamda)  
843 {  
844     double beta_rad      = deg2rad(beta);  
845     double epsilon_rad = deg2rad(epsilon);  
846  
847     return rad2deg(asin(sin(beta_rad)*cos(epsilon_rad) +  
848                     cos(beta_rad)*sin(epsilon_rad)*sin(  
849                     deg2rad(lamda))));  
850 }  
851  
852 double observer_hour_angle(double nu, double longitude, double  
853     alpha_deg)  
854 {  
855     return limit_degrees(nu + longitude - alpha_deg);  
856 }
```

```
854
855 double sun_equatorial_horizontal_parallax(double r)
856 {
857     return 8.794 / (3600.0 * r);
858 }
859
860 void right_ascension_parallax_and_topocentric_dec(double
861             latitude, double elevation,
862             double xi, double h, double delta, double *
863             delta_alpha, double *delta_prime)
864 {
865     double delta_alpha_rad;
866     double lat_rad      = deg2rad(latitude);
867     double xi_rad       = deg2rad(xi);
868     double h_rad        = deg2rad(h);
869     double delta_rad   = deg2rad(delta);
870     double u = atan(0.99664719 * tan(lat_rad));
871     double y = 0.99664719 * sin(u) + elevation*sin(lat_rad)
872             /6378140.0;
873     double x = cos(u) + elevation*cos(lat_rad)
874             /6378140.0;
875
876     delta_alpha_rad = atan2(
877         - x*sin(xi_rad)*sin(h_rad),
878         cos(delta_rad) - x*sin(xi_rad)*cos(h_rad));
```

```
874
875     *delta_prime = rad2deg( atan2(( sin(delta_rad) - y*sin(
876                         xi_rad))*cos(delta_alpha_rad),
877                         cos(delta_rad) - x*sin(xi_rad) *cos(h_rad)));
878
879 }
880
881 double topocentric_right_ascension(double alpha_deg, double
882                                     delta_alpha)
883 {
884     return alpha_deg + delta_alpha;
885 }
886
887 double topocentric_local_hour_angle(double h, double
888                                     delta_alpha)
889 {
890
891 double topocentric_elevation_angle(double latitude, double
892                                     delta_prime, double h_prime)
893 {
894     double lat_rad           = deg2rad(latitude);
895     double delta_prime_rad = deg2rad(delta_prime);
```

```
895
896     return rad2deg(asin(sin(lat_rad)*sin(delta_prime_rad) +
897                           cos(lat_rad)*cos(delta_prime_rad) * cos(
898                             deg2rad(h_prime))));
```

899

```
900 double atmospheric_refraction_correction(double pressure ,
901                                              double temperature ,
902                                              double atmos_refract , double e0)
903 {
904     double del_e = 0;
905
906     if (e0 >= -1*(SUN_RADIUS + atmos_refract))
907         del_e = (pressure / 1010.0) * (283.0 / (273.0 +
908                                         temperature)) *
909                                         1.02 / (60.0 * tan(deg2rad(e0 + 10.3/(e0 +
910                                         5.11))));
```

911

```
912 double topocentric_elevation_angle_corrected(double e0 , double
913 delta_e)
914 {
915     return e0 + delta_e;
```

```
915  }
916
917 double topocentric_zenith_angle(double e)
918 {
919     return 90.0 - e;
920 }
921
922 double topocentric_azimuth_angle_astro(double h_prime, double
923     latitude, double delta_prime)
924 {
925     double h_prime_rad = deg2rad(h_prime);
926     double lat_rad      = deg2rad(latitude);
927
928     return limit_degrees(rad2deg(atan2(sin(h_prime_rad),
929         cos(h_prime_rad)*sin(lat_rad) - tan(deg2rad(
930             delta_prime))*cos(lat_rad))));
```

```
931 }
932
933     return limit_degrees(azimuth_astro + 180.0);
934 }
935
936 double surface_incidence_angle(double zenith, double
937     azimuth_astro, double azm_rotation,
```

```
937         double slope)
938 {
939     double zenith_rad = deg2rad(zenith);
940     double slope_rad = deg2rad(slope);
941
942     return rad2deg(acos(cos(zenith_rad)*cos(slope_rad) +
943                         sin(slope_rad)*sin(zenith_rad) * cos(
944                             deg2rad(azimuth_astro -
945                             azm_rotation))));
```

```
944 }
945
946 double sun_mean_longitude(double jme)
947 {
948     return limit_degrees(280.4664567 + jme*(360007.6982779 +
949                           jme*(0.03032028 +
950                               jme*(1/49931.0      + jme*(-1/15300.0      +
951                                   jme*(-1/2000000.0))))));
```

```
950 }
951
952 double eot(double m, double alpha, double del_psi, double
953 epsilon)
954 {
955     return limit_minutes(4.0*(m - 0.0057183 - alpha + del_psi*
956                           cos(deg2rad(epsilon))));
```

```
955 }
```

```
956
957 double approx_sun_transit_time(double alpha_zero, double
958   longitude, double nu)
959   return (alpha_zero - longitude - nu) / 360.0;
960 }
961
962 double sun_hour_angle_at_rise_set(double latitude, double
963   delta_zero, double h0_prime)
964 {
965   double h0 = -99999;
966   double latitude_rad = deg2rad(latitude);
967   double delta_zero_rad = deg2rad(delta_zero);
968   double argument = (sin(deg2rad(h0_prime)) - sin(
969     latitude_rad)*sin(delta_zero_rad)) /
970       (cos(latitude_rad)*cos(delta_zero_rad));
971
972   if (fabs(argument) <= 1) h0 = limit_degrees180(rad2deg(
973     acos(argument)));
974
975 void approx_sun_rise_and_set(double *m_rts, double h0)
976 {
```

```
977     double h0_dfrac = h0/360.0;
978
979     m_rts[SUN_RISE]    = limit_zerozone(m_rts[SUN_TRANSIT] -
980                                         h0_dfrac);
980     m_rts[SUN_SET]     = limit_zerozone(m_rts[SUN_TRANSIT] +
981                                         h0_dfrac);
981     m_rts[SUN_TRANSIT] = limit_zerozone(m_rts[SUN_TRANSIT]);
982 }
983
984 double rts_alpha_delta_prime(double *ad, double n)
985 {
986     double a = ad[JD_ZERO] - ad[JD_MINUS];
987     double b = ad[JD_PLUS] - ad[JD_ZERO];
988
989     if (fabs(a) >= 2.0) a = limit_zerozone(a);
990     if (fabs(b) >= 2.0) b = limit_zerozone(b);
991
992     return ad[JD_ZERO] + n * (a + b + (b-a)*n)/2.0;
993 }
994
995 double rts_sun_altitude(double latitude, double delta_prime,
996                           double h_prime)
997 {
998     double latitude_rad      = deg2rad(latitude);
999     double delta_prime_rad  = deg2rad(delta_prime);
```

999

```
1000      return rad2deg(asin(sin(latitude_rad)*sin(delta_prime_rad))
```

+

```

1001           cos( latitude_rad ) *cos( delta_prime_rad )

$$* \cos( \text{deg2rad}( h_{\text{prime}} ) ) );$$


```

1002 }

1003

```
1004 double sun_rise_and_set(double *m_rts, double *h_rts,
```

```
double *delta_prime , double latitude ,
```

```
1005           double *h_prime, double h0_prime, int  
1006             sun)
```

1006 {

```
1007      return m_rts[sun] + (h_rts[sun] - h0_prime) /
```

```
1008     (360.0*cos(deg2rad(delta_prime[sun]))*cos(deg2rad(
1009         latitude))*sin(deg2rad(h_prime[sun]))));
```

1009 }

1010

1011 //

1012 // Calculate required SPA parameters to get the right
ascension (alpha) and declination (delta)

1013 // Note: JD must be already calculated and in structure

1014 //

```
1015 void calculate_geocentric_sun_right_ascension_and_declination(
1016     spa_data *spa)
1017 {
1018     double x[TERM_X_COUNT];
1019     spa->jc = julian_century(spa->jd);
1020
1021     spa->jde = julian_ephemeris_day(spa->jd, spa->delta_t);
1022     spa->jce = julian_ephemeris_century(spa->jde);
1023     spa->jme = julian_ephemeris_millennium(spa->jce);
1024
1025     spa->l = earth_heliocentric_longitude(spa->jme);
1026     spa->b = earth_heliocentric_latitude(spa->jme);
1027     spa->r = earth_radius_vector(spa->jme);
1028
1029     spa->theta = geocentric_longitude(spa->l);
1030     spa->beta = geocentric_latitude(spa->b);
1031
1032     x[TERM_X0] = spa->x0 = mean_elongation_moon_sun(spa->jce);
1033     x[TERM_X1] = spa->x1 = mean_anomaly_sun(spa->jce);
1034     x[TERM_X2] = spa->x2 = mean_anomaly_moon(spa->jce);
1035     x[TERM_X3] = spa->x3 = argument_latitude_moon(spa->jce);
1036     x[TERM_X4] = spa->x4 = ascending_longitude_moon(spa->jce);
1037
```



```
1053 // Calculate Equation of Time (EOT) and Sun Rise , Transit , &
      Set (RTS)

1054 //

1055

1056 void calculate_eot_and_sun_rise_transit_set(spa_data *spa)
1057 {
1058     spa_data sun_rts;
1059     double nu, m, h0, n;
1060     double alpha[JD_COUNT], delta[JD_COUNT];
1061     double m_rts[SUN_COUNT], nu_rts[SUN_COUNT], h_rts[
1062         SUN_COUNT];
1063     double alpha_prime[SUN_COUNT], delta_prime[SUN_COUNT],
1064         h_prime[SUN_COUNT];
1065     double h0_prime = -1*(SUN_RADIUS + spa->atmos_refract);
1066     int i;
1067
1068     sun_rts = *spa;
1069     m = sun_mean_longitude(spa->jme);
1070     spa->eot = eot(m, spa->alpha, spa->del_psi, spa->epsilon);
1071     sun_rts.hour = sun_rts.minute = sun_rts.second = 0;
1072     sun_rts.delta_ut1 = sun_rts.timezone = 0.0;
```

```
1073     sun_rts.jd = julian_day (sun_rts.year,     sun_rts.month,
1074                               sun_rts.day,        sun_rts.hour,
1074                               sun_rts.minute,    sun_rts.second,
1074                               sun_rts.delta_ut1, sun_rts.
1074                               timezone);
1075
1076     calculate_geocentric_sun_right_ascension_and_declination(&
1076                     sun_rts);
1077     nu = sun_rts.nu;
1078
1079     sun_rts.delta_t = 0;
1080     sun_rts.jd--;
1081     for (i = 0; i < JD_COUNT; i++) {
1082         calculate_geocentric_sun_right_ascension_and_declination
1082             (&sun_rts);
1083         alpha[i] = sun_rts.alpha;
1084         delta[i] = sun_rts.delta;
1085         sun_rts.jd++;
1086     }
1087
1088     m_rts[SUN_TRANSIT] = approx_sun_transit_time(alpha[JD_ZERO
1088                 ], spa->longitude, nu);
1089     h0 = sun_hour_angle_at_rise_set(spa->latitude, delta[
1089                 JD_ZERO], h0_prime);
```

```
1091      if (h0 >= 0) {  
1092  
1093          approx_sun_rise_and_set(m_rts, h0);  
1094  
1095          for (i = 0; i < SUN_COUNT; i++) {  
1096              nu_rts[i] = nu + 360.985647*m_rts[i];  
1097  
1098              n = m_rts[i] + spa->delta_t/86400.0;  
1099              alpha_prime[i] = rts_alpha_delta_prime(alpha, n);  
1100              delta_prime[i] = rts_alpha_delta_prime(delta, n);  
1101  
1102              h_prime[i] = limit_degrees180pm(nu_rts[i] +  
1103                                          spa->longitude - alpha_prime[i]);  
1104  
1105              h_rts[i] = rts_sun_altitude(spa->latitude,  
1106                                         delta_prime[i], h_prime[i]);  
1107  
1108              spa->srha = h_prime[SUN_RISE];  
1109              spa->ssha = h_prime[SUN_SET];  
1110              spa->sta = h_rts[SUN_TRANSIT];  
1111  
1112              spa->suntransit = dayfrac_to_local_hr(m_rts[  
SUN_TRANSIT] - h_prime[SUN_TRANSIT] / 360.0,
```



```
1129 int spa_calculate(spa_data *spa)
1130 {
1131     int result;
1132
1133     result = validate_inputs(spa);
1134
1135     if (result == 0)
1136     {
1137         spa->jd = julian_day(spa->year,     spa->month,    spa->
1138                               day,           spa->hour,
1139                               spa->minute,   spa->second,   spa->
1140                               delta_ut1,   spa->timezone);
1141
1142         spa->h = observer_hour_angle(spa->nu, spa->longitude,
1143                                       spa->alpha);
1144
1145         spa->xi = sun_equatorial_horizontal_parallax(spa->r);
1146
1147         right_ascension_parallax_and_topocentric_dec(spa->
1148                           latitude, spa->elevation, spa->xi,
1149                           spa->h,   spa->delta,  &(spa->
1150                           del_alpha), &(spa->
```

```
                                delta_prime));  
1147  
1148     spa->alpha_prime = topocentric_right_ascension(spa->  
           alpha, spa->del_alpha);  
1149     spa->h_prime      = topocentric_local_hour_angle(spa->h  
           , spa->del_alpha);  
1150  
1151     spa->e0          = topocentric_elevation_angle(spa->  
           latitude, spa->delta_prime, spa->h_prime);  
1152     spa->del_e        = atmospheric_refraction_correction(spa->  
           pressure, spa->temperature,  
1153                                         spa->  
                                         atmos_refract  
                                         ,  
                                         spa  
                                         ->  
                                         e0  
                                         );  
1154     spa->e          = topocentric_elevation_angle_corrected(  
           spa->e0, spa->del_e);  
1155  
1156     spa->zenith      = topocentric_zenith_angle(spa->e);  
1157     spa->azimuth_astro = topocentric_azimuth_angle_astro(  
           spa->h_prime, spa->latitude,
```

1158

Listing I.6: SPA Source File